

# ECSE 6520: Detection and Estimation Theory

## Homework 2

Due February 13th, 2014

1. Prove that if  $T_{min}$  is a minimal sufficient statistics and  $h$  is an invertible function, then  $h(T_{min})$  is also a minimal sufficient statistics.
2. Let  $T$  be a sufficient statistics distributed as  $T \sim \mathcal{B}(2, \theta)$  where  $\mathcal{B}(2, \theta)$  denotes the binomial distribution with parameters  $n$  (number of trials) and  $\theta$  (probability of success). Show that  $T$  is a complete sufficient statistics.
3. Show that each of the following statistics is not complete, by finding a non-zero function  $\phi$  such that  $E[\phi(T)] = 0$ .
  - a.  $T$  is uniformly distributed between  $-\theta$  and  $\theta$ .
  - b.  $T \sim \mathcal{N}(0, \theta)$ .
4. Express the following pdfs or pmfs as members of the exponential family of distributions and determine the minimal sufficient statistics. For each item assume  $N$  i.i.d. random variables.
  - a. Exponential pdf.
  - b. Rayleigh pdf.
  - c. Multinomial pmf.
  - d. Geometric pmf.