

ECSE 2010
Electric Circuits
Fall 2006 - Millard
Exam 1

Name Solutions Only

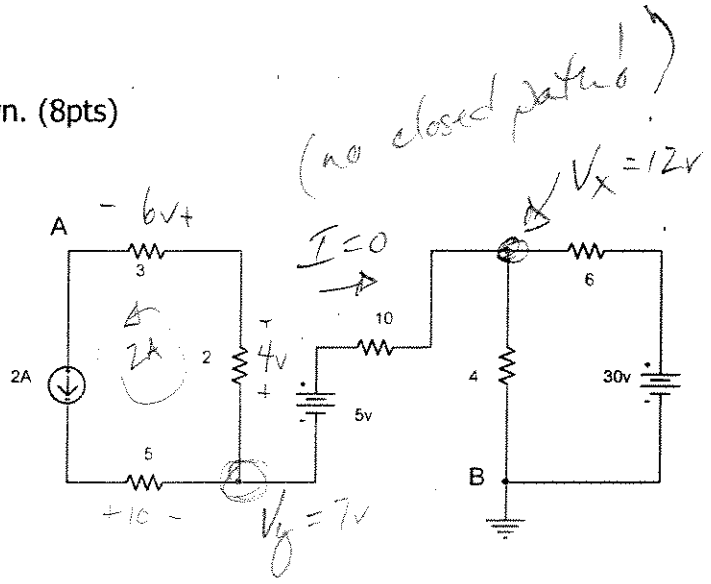
| Problem No. | Pts. | Score |
|-------------|--------|-------|
| 1 | 20pts | x/20 |
| 2 | 20pts | x/20 |
| 3 | 20pts | x/20 |
| 4 | 20pts | x/20 |
| 5 | 20pts | x/20 |
| Total | 100pts | x/100 |

Please Note:

- * Please place your answers in the spaces provided.
- * You must show your work to receive credit.

Problem 1 (20pts)

a.) Find V_{AB} in the circuit shown. (8pts)



$$V_B = 0$$

$$V_x = \frac{4}{4+6} \times 30 = 12v$$

$$V_y = 12 - 5 = 7v$$

$$V_A = V_y - 4v - 6v = 7v - 10v$$

$$V_A = -3v$$

$$V_{AB} = -3 - 0 = -3v$$

3pts →

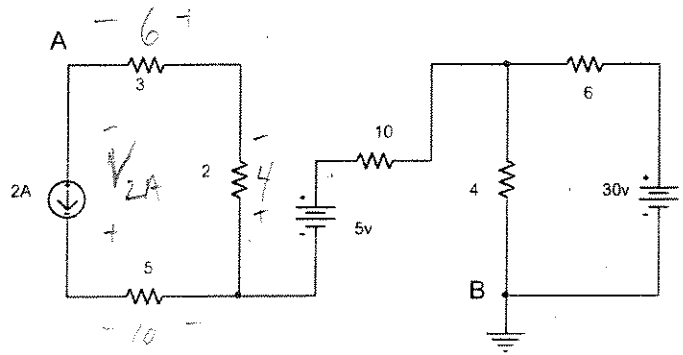
3pts →

2pts →

| | |
|----------|-------|
| V_{AB} | $-3v$ |
|----------|-------|

Problem 1 (cont)

b.) Find the power supplied/absorbed by the 2A source, 5v source and 4Ω resistor in the circuit shown. (12pts)



①

$$|P_{2A}| = |V_{2A}| \times |2A|$$

$$V_{2A} = 20$$

$$|P_{2A}| = 20 \times 2 = 40W$$

$$P_{2A} = -40W \text{ (supply)} \quad (3 \text{ pts})$$

② ~~$|P_{5V}| = |V_5| \times |I_5| \rightarrow 0$~~

$$P_{5V} = 5 \times 0 = 0 \quad (3 \text{ pts})$$

③ $P_{4\Omega} = V_4 \times I_4$

$$V_4 = \frac{4}{4+6} \times 30 = 12V$$

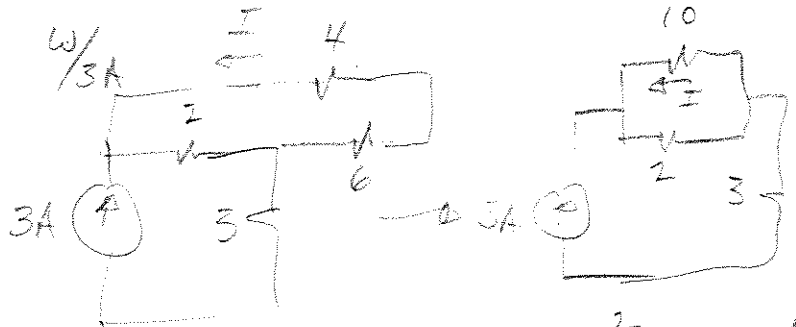
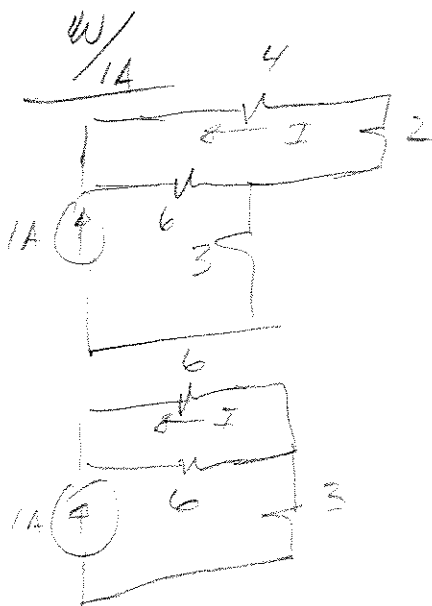
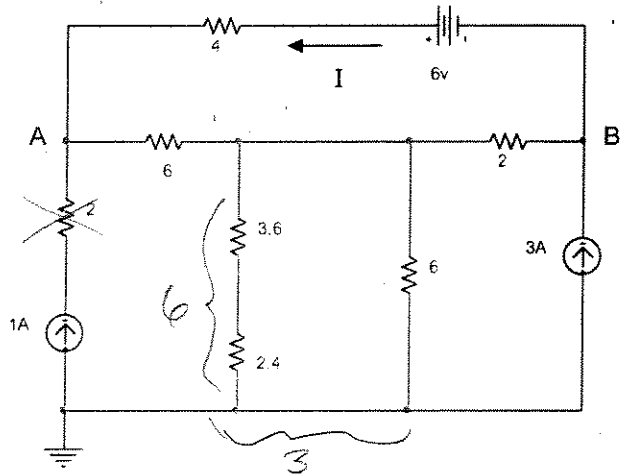
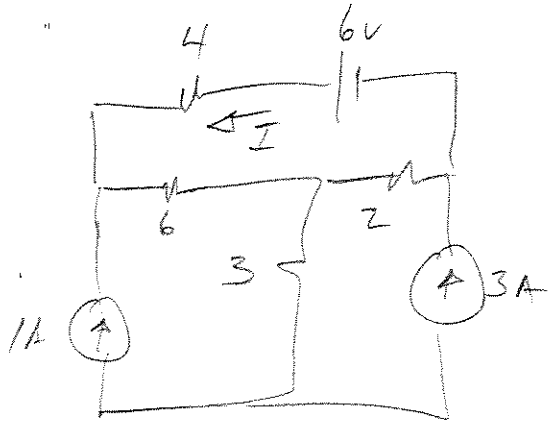
$$I_4 = \frac{V_4}{4} = 3A$$

$$P_4 = 12 \times 3 = 36W \quad (3 \text{ pts})$$

| | |
|---------------|------|
| P_{2A} | -40W |
| P_{5V} | 0W |
| $P_{4\Omega}$ | 36W |

Problem 2 (20pts)

a.) Find I (through the 4Ω resistor) due to each of the sources using superposition for the circuit shown. (15pts)

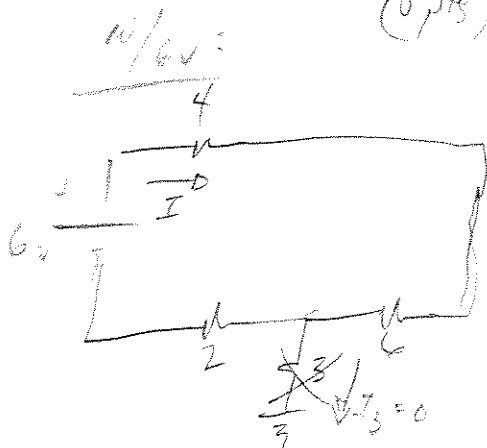


$$I = 3A \cdot \frac{2}{2+10} = \frac{1}{2}A$$

(5pts)

$$I = -\frac{1A}{2} = .5A \text{ (opposite direction)}$$

(5pts)



$$I = \frac{6V}{8+4} = \frac{6}{12}$$

$$I = +.5A$$

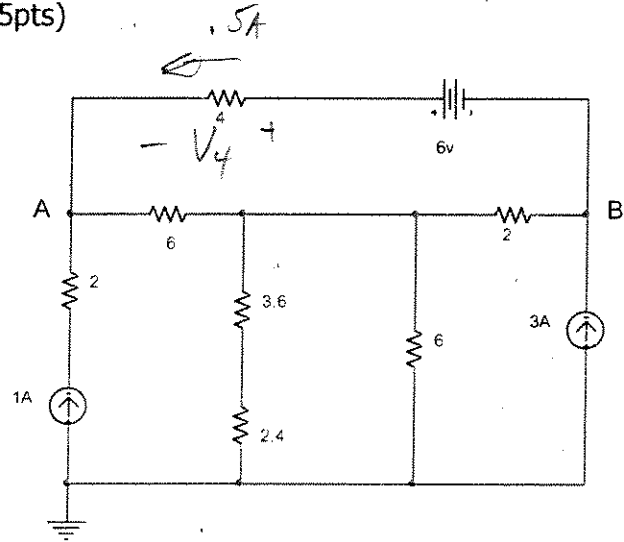
(5pts)

| | |
|--------|------|
| I (1A) | -.5A |
| I (3A) | +.5A |
| I (6V) | +.5A |

$$I_{TOT} = +.5A$$

Problem 2 (cont)

b.) Find V_{AB} in the circuit shown. (5pts)



$$V_4 = I_{TOTAL} \times 4$$

$$V_4 = 4 \times .5 = 2V$$

$$V_{AB} = V_A - V_B$$

$$V_{AB} = 6V - V_4 = 6 - (.5 \times 4) = 6 - 2 = 4V$$

(5pts)

| | |
|----------|----|
| V_{AB} | 4V |
|----------|----|

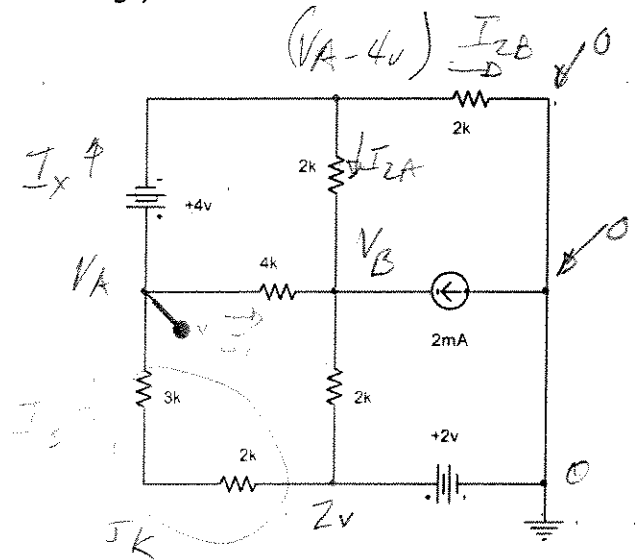
Problem 3 (20pts)

Find V (at the probe) for the circuit shown using your choice of either mesh or nodal analysis.

$$I_x = I_{2A} + I_{2B}$$

$$I_x = \frac{(V_A - 4) - V_B}{2k} + \frac{(V_A - 4) - 0}{2k}$$

$$I_x = \frac{2V_A - 8 - V_B}{2k}$$



a) V_A :

$$\frac{V_A - V_B}{4k} + \frac{V_A - 2}{5k} + \frac{2V_A - 8 - V_B}{2k} = 0$$

$(\times 20k)$ $5V_A - 5V_B + 4V_A - 8 + 20V_A - 80 - 10V_B = 0$

① $29V_A - 15V_B = 88$

a) V_B

$$\frac{V_B - V_A}{4k} + \frac{V_B - 2}{2k} + \frac{V_B - (V_A - 4)}{2k} - 2mA = 0$$

$(\times 4k)$ $V_B - V_A + 2V_B - 4 + 2V_B - 2V_A + 8 - 8 = 0$

② $-3V_A + 5V_B = 4$

$$\begin{cases} -9V_A + 15V_B = 12 & (3) \\ 29V_A - 15V_B = 88 & (1) \end{cases}$$

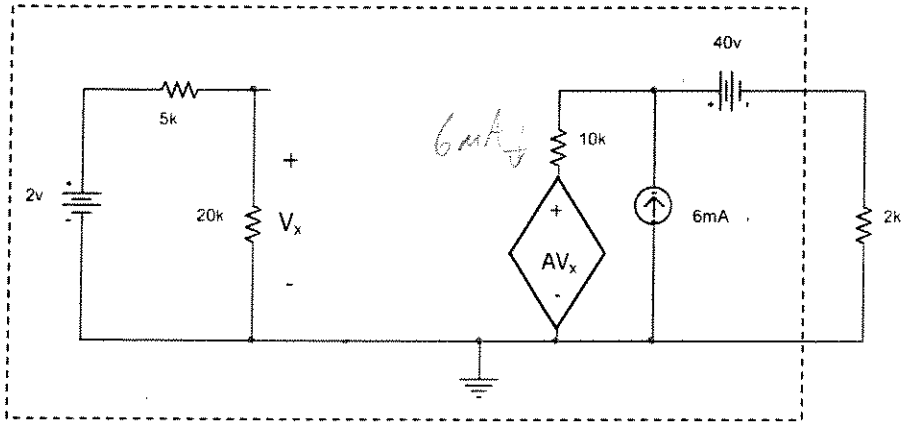
$$20V_A + 0V_B = 100$$

Thus: $V_A = 5$

| | |
|---|----|
| V | 5V |
|---|----|

Problem 4 (20pts)

Given the following circuit:



a.) Find V_{TH} , the open circuit (without the 2K) output voltage of the circuit in the dashed line, if $A=100$. (8pts)

V_{TH} :

$$V_x = \frac{20k}{25k} \times 2V = \frac{8}{5} V$$

$$AV_x = 100 \times \frac{8}{5} = 160$$

$$V_{oc} = AV_x + (6mA)10k - 40V$$

$$V_{oc} = V_{TH} = 160 + 60 - 40$$

$$V_{TH} = 180$$

R_{TH} :

10k + 2k = 12k

6mA + 12k = 12k

| | |
|----------|------|
| V_{TH} | 180V |
|----------|------|

$$I_{sc} = 6mA + I_{oc} = 6mA + \frac{180 - 40}{12k}$$

$$I_{sc} = 6mA + \frac{140}{12k} = 17mA$$

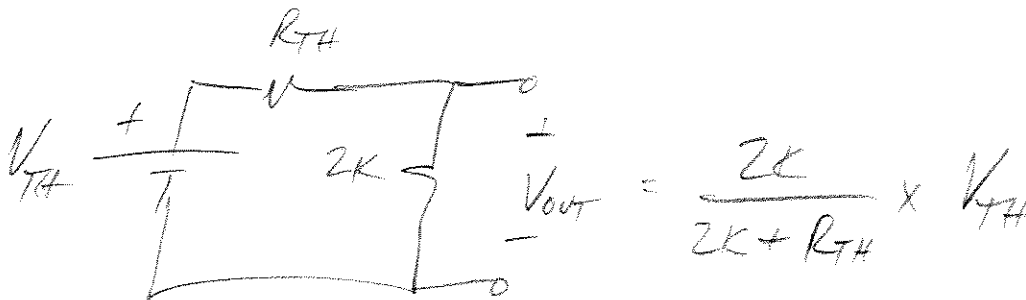
Problem 4 (cont)

b.) Find the equivalent resistance (R_{TH}) that a multimeter would read across the two wires that exit the dashed line (to the right of the 2K resistor; but not including the 2K resistor) if $A=100$. (8pts)

$$R_{TH} = \frac{V_{TH}}{I_{SC}} = \frac{180V}{18mA} = 10K$$

| | |
|----------|-----|
| R_{TH} | 10K |
|----------|-----|

c.) Find V_{out} across the 2k resistor at the output of above circuit if $A=100$. (4pts)

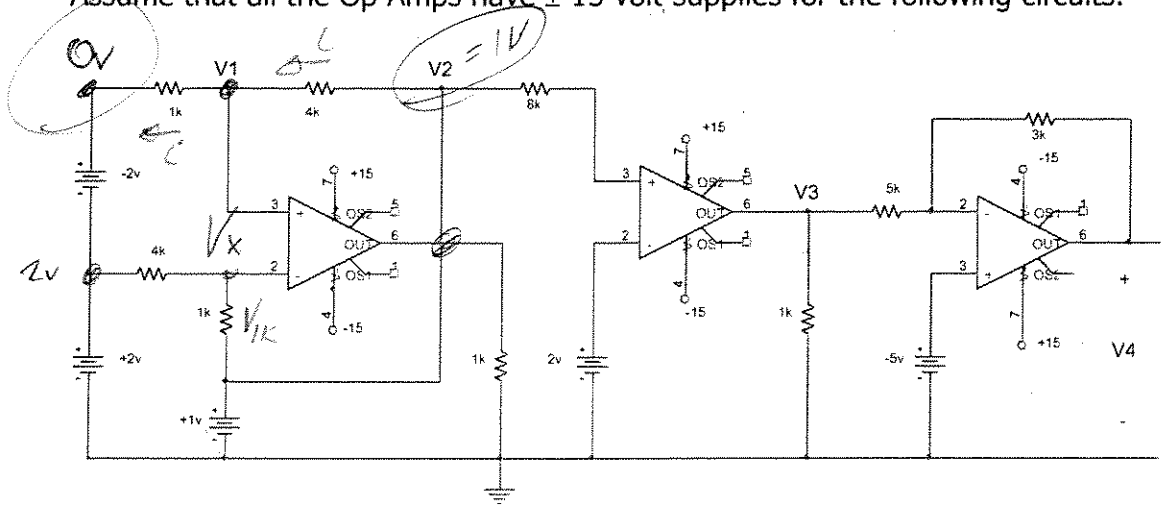


$$V_{out} = \frac{2}{12} \times 180 = 30V$$

| | |
|-----------|-----|
| V_{out} | 30V |
|-----------|-----|

Problem 5 (20pts)

Assume that all the Op Amps have ± 15 volt supplies for the following circuits.



a.) Find V_1 & V_2 in the above circuit. (10pts)

$$V_x = V_{1k} + 1V$$

$$V_{1k} = \frac{1k}{1k+4k} (2V - 1V) = \frac{1}{5} V$$

$$V_x = 1.2V$$

$$4 \frac{V_1 - 0}{1k} = \frac{V_2 - V_1}{4k} \quad (\text{no } I \text{ into the op amp})$$

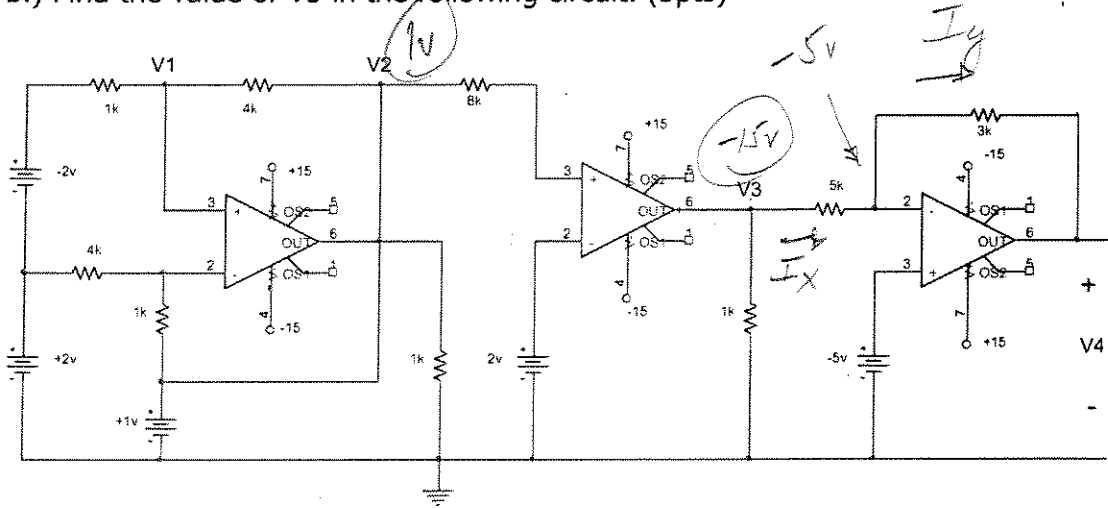
$$V_1 = \frac{V_2}{5} = \frac{1}{5} = .2V$$

Thus:
 $V_1 \neq V_x$!

| | |
|-------|-----|
| V_1 | .2V |
| V_2 | 1V |

Problem 5 (cont)

b.) Find the value of V3 in the following circuit. (5pts)



$$V_3 = V_D \times \infty = (1-2) \times (\infty) = -\infty \rightarrow -15v$$

| | |
|----|------|
| V3 | -15v |
|----|------|

c.) Find V4 in the above circuit. (5pts)

$$I_x = I_y$$

$$I_x = \frac{-15 - (-5v)}{5K} \quad ; \quad I_y = \frac{-5v - V_4}{3K}$$

$$5 + 3K \left(\frac{-10}{5K} \right) = -V_4$$

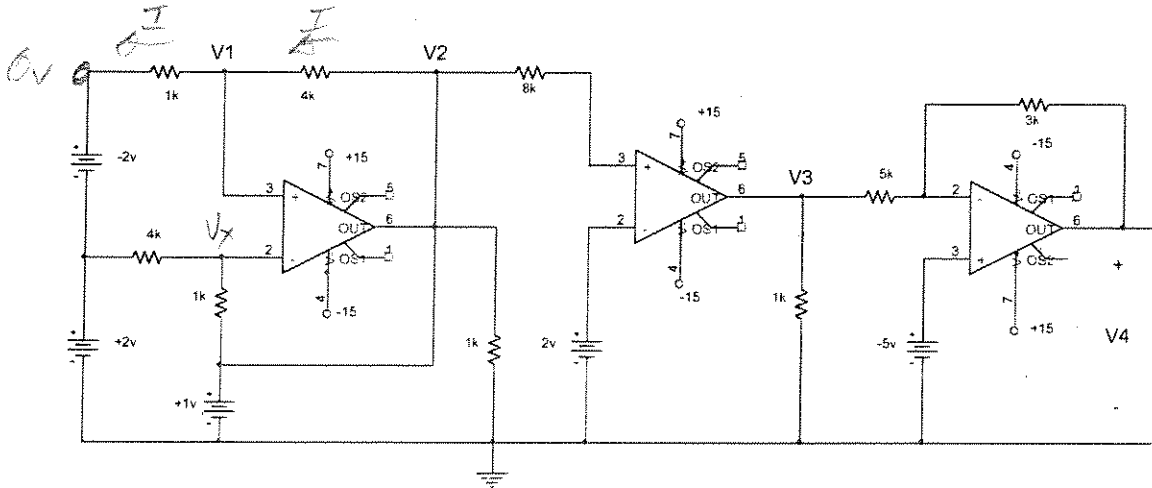
$$V_4 = 6 - 5 = 1v$$

| | |
|----|----|
| V4 | 1v |
|----|----|

WRONG
BUT OK

Problem 5 (20pts)

Assume that all the Op Amps have ± 15 volt supplies for the following circuits.



a.) Find V1 & V2 in the above circuit. (10pts)

Assuming neg fdbk (which is holding $V_x \rightarrow 0$)

$$V_1 = V_x$$

$$V_x = \left[(2-1) \times \frac{1k}{1k+4k} \right] + 1v = 1.2v$$

so...

$$V_1 \text{ should be } = 1.2v$$

If so:

$$\frac{V_1 - 0}{1k} = \frac{V_2 - V_1}{4k}$$

$$4V_1 + V_1 = V_2$$

$V_2 = 6v$ but is connected to the 1v source.

If $V_2 = 6v$

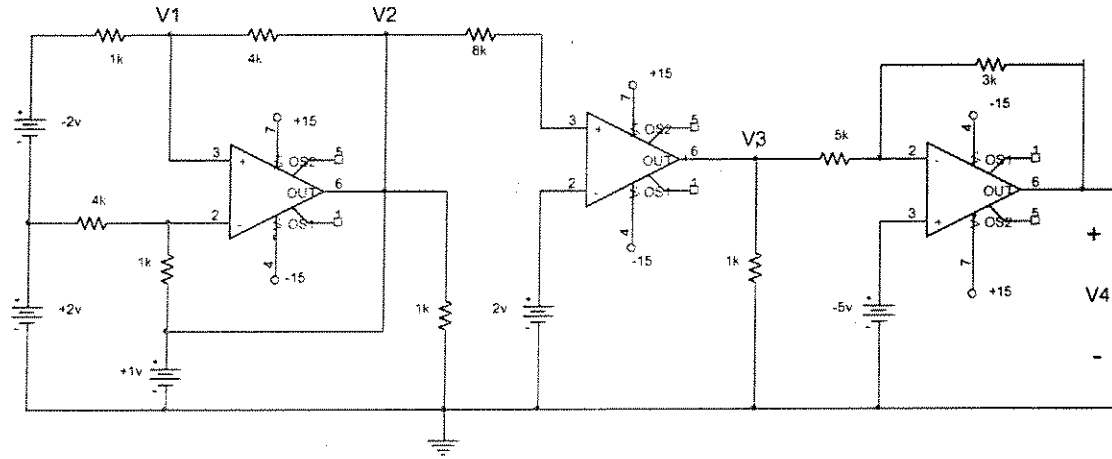
| | |
|----|-----|
| V1 | 1.2 |
| V2 | 6v |

WRONG
BUT OK

Problem 5 (cont)

WRONG
BUT OK

b.) Find the value of V3 in the following circuit. (5pts)



$$V_3 = (V_2 - 2V) \times \frac{5k}{3k} \quad (\text{no fdbk})$$

$$V_3 = +15V$$

| | |
|----|-----|
| V3 | +15 |
|----|-----|

WRONG
BUT
OK

c.) Find V4 in the above circuit. (5pts)

$$\frac{V_3 - (-5V)}{5k} = \frac{(-5 - V_4)}{3k}$$

$$12 = -5 - V_4$$

$$V_4 = -5 - 12 = -17$$

-15

| | |
|----|------|
| V4 | -15V |
|----|------|

WRONG
BUT
OK