

ECSE 2010
Electric Circuits
Fall 2006 - **Millard**
Exam 2

Name _____

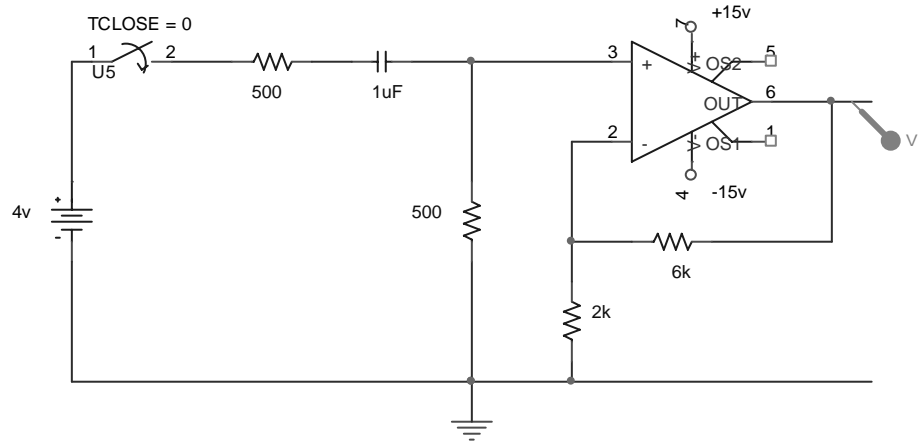
Problem No.	Pts.	Score
1	10pts	
2	25pts	
3	25pts	
4	20pts	
5	20pts	
Total	100pts	

Please Note:

- * Please place your answers in the spaces provided.
- * You must show your work to receive credit.

Problem 1 (10pts)

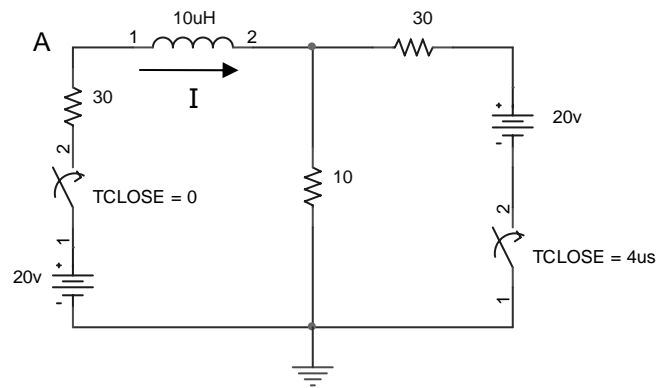
Find $V(t)$ in the circuit shown for $t \geq 0$.



$V(t)$	
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Problem 2 (25pts)

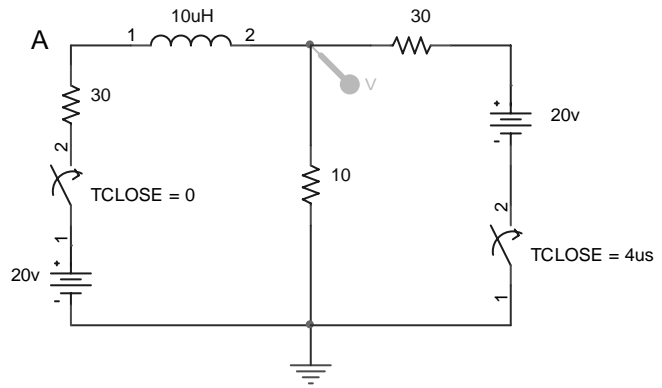
a.) Find I (through the $10\mu\text{H}$ inductor) at each of the times indicated for the circuit shown. (15pts)



I ($1\mu\text{s}$)	
I ($4\mu\text{s}$)	
I ($8\mu\text{s}$)	

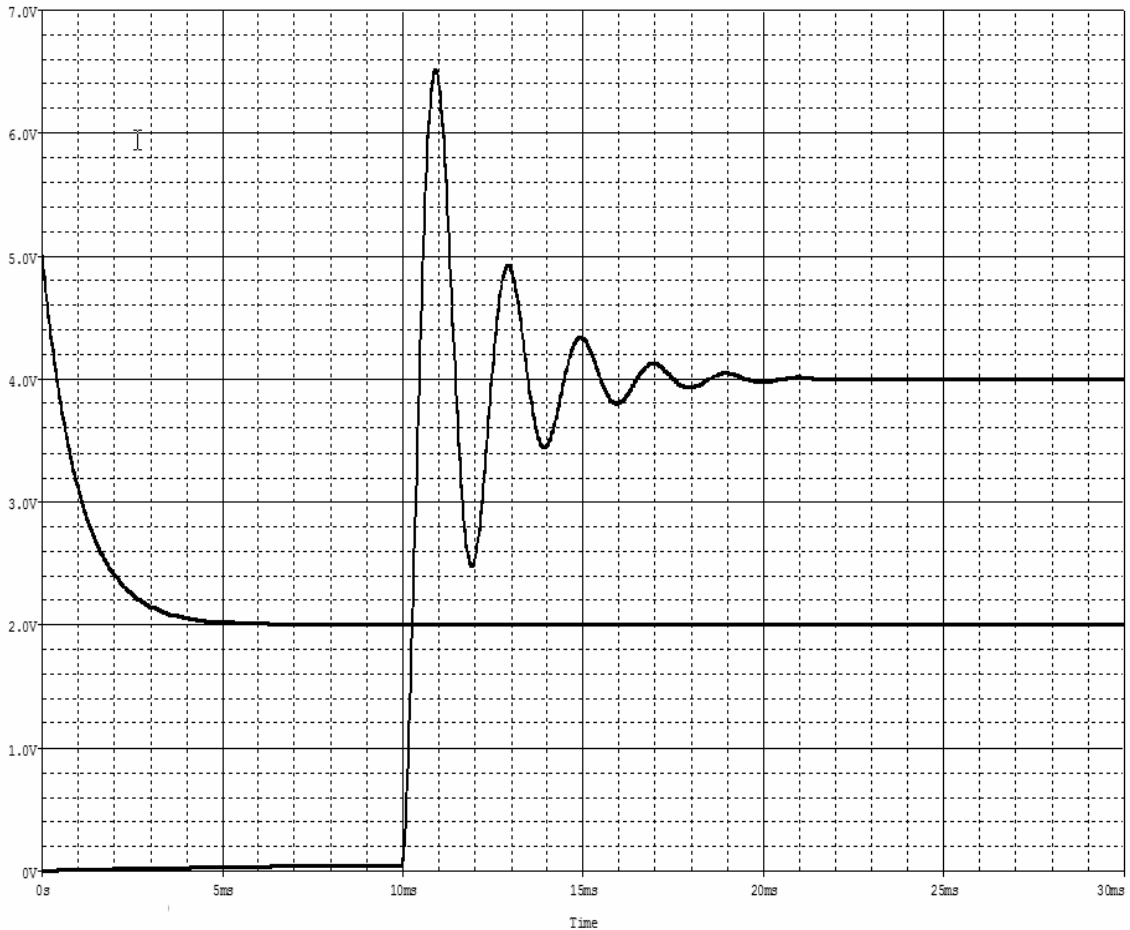
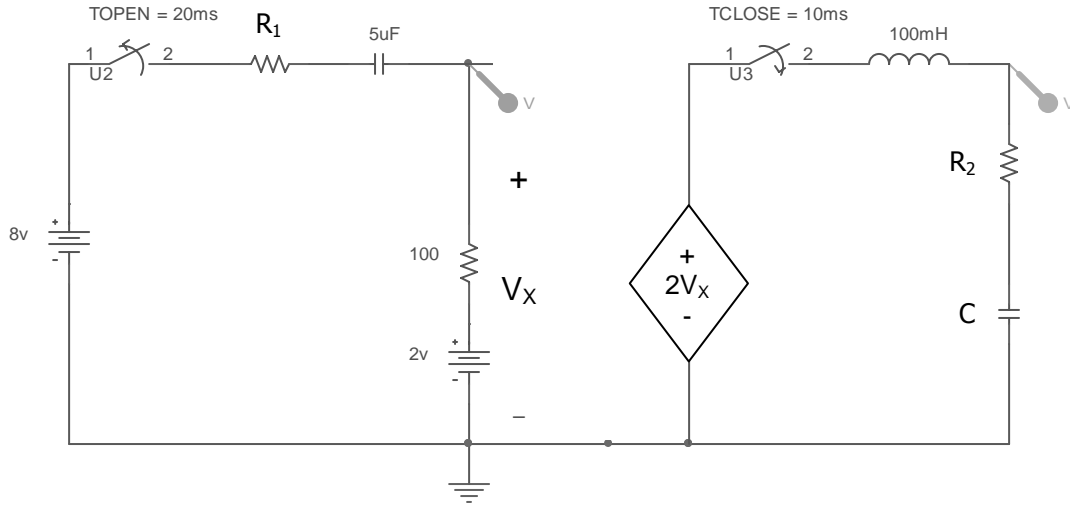
Problem 2 (cont)

b.) Sketch $V(t)$ (across the 10ohm resistor) for $0 \leq t < 10\mu s$; showing ALL pertinent values at the critical points in time. (10pts)



Problem 3 (25pts)

Given the corresponding plots for the circuit shown; find the values of the circuit's components (R_1 , R_2 , and C).

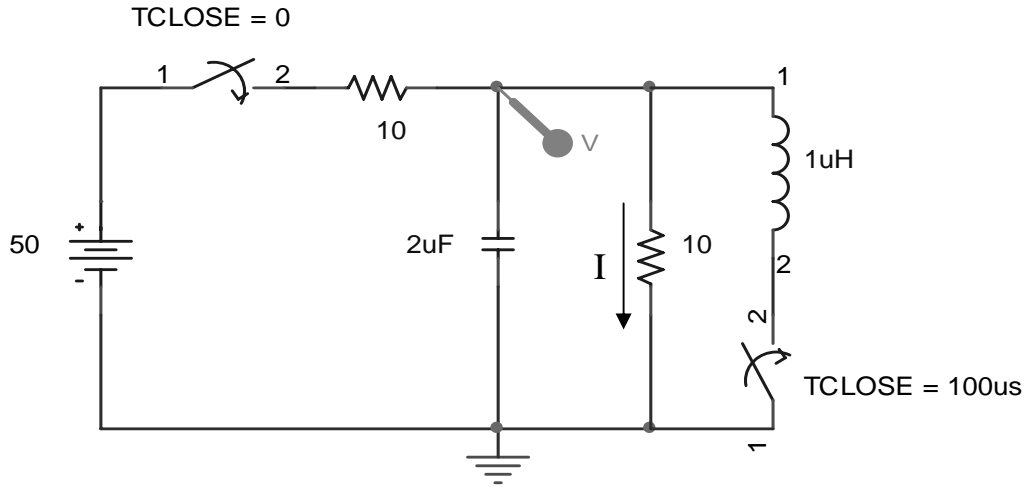


Problem 3 (cont)

R ₁ (5pts)	
R ₂ (10pts)	
C (10pts)	

Problem 4 (20pts)

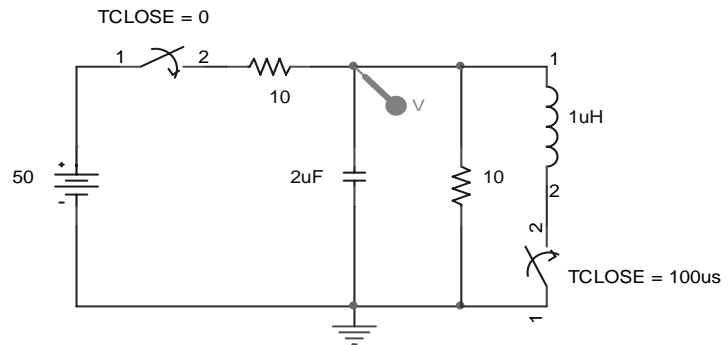
Given the following circuit find $I(100\mu\text{s}^-)$, $V(100\mu\text{s}^+)$, $I(\infty)$ and $V(\infty)$. Please provide justification for your responses.



$I(0^-)$	
$V(0^-)$	
$I(\infty)$	
$V(\infty)$	

Problem 5 (20pts)

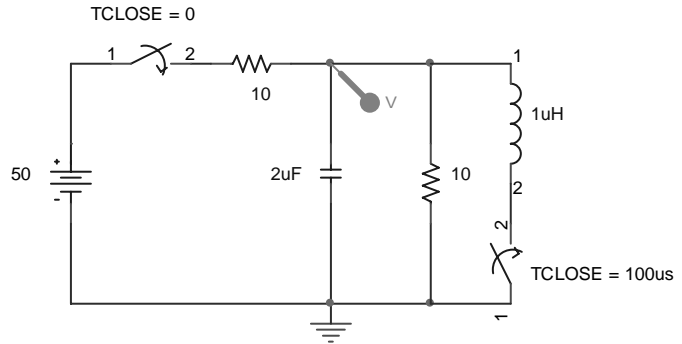
a.) Find $V(t)$ (across the capacitor) in the circuit shown for $t < 100\mu\text{s}$. (5pts)



$V(t)$	
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Problem 5 (cont)

b.) Find the response type (over, critically, or under) and $V(t)$ (across the capacitor) in the circuit shown for $t > 100\mu s$. (15pts)



Type	
$V(t)$	

Extra space (if needed)

Name _____

Extra space (if needed)

Name _____

Item no.	$f(t)$	$F(s)$
1.	$\delta(t)$	1
2.	$u(t)$	$\frac{1}{s}$
3.	$tu(t)$	$\frac{1}{s^2}$
4.	$t^n u(t)$	$\frac{n!}{s^{n+1}}$
5.	$e^{-at}u(t)$	$\frac{1}{s+a}$
6.	$\sin \omega t u(t)$	$\frac{\omega}{s^2 + \omega^2}$
7.	$\cos \omega t u(t)$	$\frac{s}{s^2 + \omega^2}$

Item no.	Theorem	Name
1.	$\mathcal{L}[f(t)] = F(s) = \int_{0^-}^{\infty} f(t)e^{-st} dt$	Definition
2.	$\mathcal{L}[kf(t)] = kF(s)$	Linearity theorem
3.	$\mathcal{L}[f_1(t) + f_2(t)] = F_1(s) + F_2(s)$	Linearity theorem
4.	$\mathcal{L}[e^{-at}f(t)] = F(s+a)$	Frequency shift theorem
5.	$\mathcal{L}[f(t-T)] = e^{-sT}F(s)$	Time shift theorem
6.	$\mathcal{L}[f(at)] = \frac{1}{a}F\left(\frac{s}{a}\right)$	Scaling theorem
7.	$\mathcal{L}\left[\frac{df}{dt}\right] = sF(s) - f(0^-)$	Differentiation theorem
8.	$\mathcal{L}\left[\frac{d^2f}{dt^2}\right] = s^2F(s) - sf(0^-) - \dot{f}(0^-)$	Differentiation theorem
9.	$\mathcal{L}\left[\frac{d^nf}{dt^n}\right] = s^nF(s) - \sum_{k=1}^n s^{n-k}f^{k-1}(0^-)$	Differentiation theorem
10.	$\mathcal{L}\left[\int_{0^-}^t f(\tau) d\tau\right] = \frac{F(s)}{s}$	Integration theorem
11.	$f(\infty) = \lim_{s \rightarrow 0} sF(s)$	Final value theorem ¹
12.	$f(0^+) = \lim_{s \rightarrow \infty} sF(s)$	Initial value theorem ²

¹ For this theorem to yield correct finite results, all roots of the denominator of $F(s)$ must have negative real parts and no more than one can be at the origin.

² For this theorem to be valid, $f(t)$ must be continuous or have a step discontinuity at $t = 0$ (i.e., no impulses or their derivatives at $t = 0$).