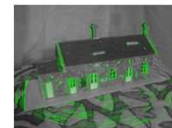
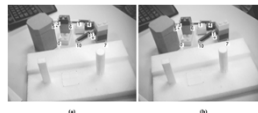
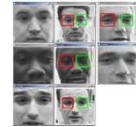


Scale Invariant Feature Transform

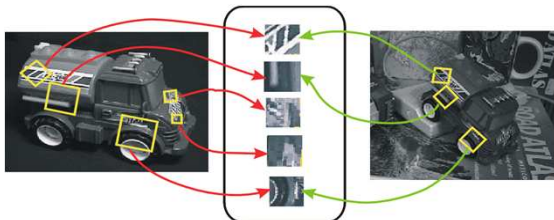
Why do we care about matching features?

- Camera calibration
- Stereo
- Tracking/SFM
- Image mosaicing
- Object/activity Recognition
- ...



Objection representation and recognition

- Image content is transformed into local feature coordinates that are invariant to translation, rotation, scale, and other imaging parameters



- Automatic Mosaicing
- <http://www.cs.ubc.ca/~mbrown/autostitch/autostitch.html>



We want invariance!!!

- To illumination
- To scale
- To rotation
- To affine
- To perspective projection

Types of invariance

- Illumination



Types of invariance

- Illumination
- Scale



Types of invariance

- Illumination
- Scale
- Rotation



Types of invariance

- Illumination
- Scale
- Rotation
- Affine



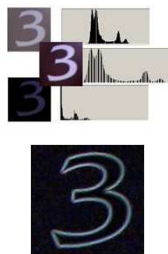
Types of invariance

- Illumination
- Scale
- Rotation
- Affine
- Full Perspective



How to achieve illumination invariance

- The easy way (normalized)
- Difference based metrics (random tree, Haar, and sift, gradient)



How to achieve scale invariance

- Pyramids
 - Divide width and height by 2
 - Take average of 4 pixels for each pixel (or Gaussian blur with different σ)
 - Repeat until image is tiny
 - Run filter over each size image and hope its robust
- Scale Space (DOG method)

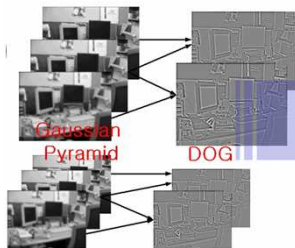
Pyramids



How to achieve scale invariance

- Scale Space: Difference of Gaussian (DOG)
 - Take features from differences of these images- producing the gradient image
 - If the feature is repeatedly present in between Difference of Gaussians, it is Scale Invariant and should be kept.

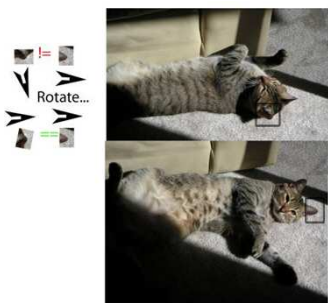
Differences Of Gaussians



Rotation Invariance

- Rotate all features to go the same way in a determined manner
- Take histogram of Gradient directions. Rotate to most dominant (maybe second if its good enough, sub-Bin accuracy)

Rotation Invariance



Affine Invariance

- Easy way: Warp your training and hope
- Fancy way: design your feature itself to be robust against affine transformations (SIFT method)

SIFT algorithm overview

- Scale-space extrema detection
 - Get tons of points from maxima+minima of DOGS
- Keypoint localization
 - Threshold on simple contrast (low contrast is generally less reliable than high for feature points)
 - Threshold based on principal curvatures
 - Orientation assignment
- Keypoint descriptor
 - Construct histograms of gradients (HOG)

Scale-space extrema detection

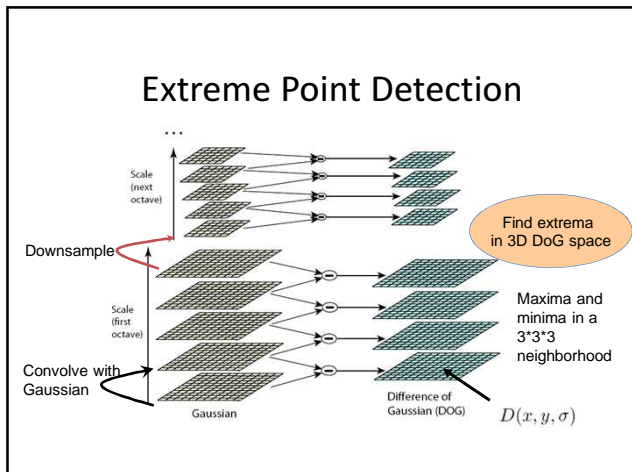
- Find the points, whose surrounding patches (with some scale) are distinctive
- An approximation to the scale-normalized Difference of Gaussian

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2+y^2)/2\sigma^2}$$

$$D(x, y, \sigma) = (G(x, y, k\sigma) - G(x, y, \sigma)) * I(x, y)$$

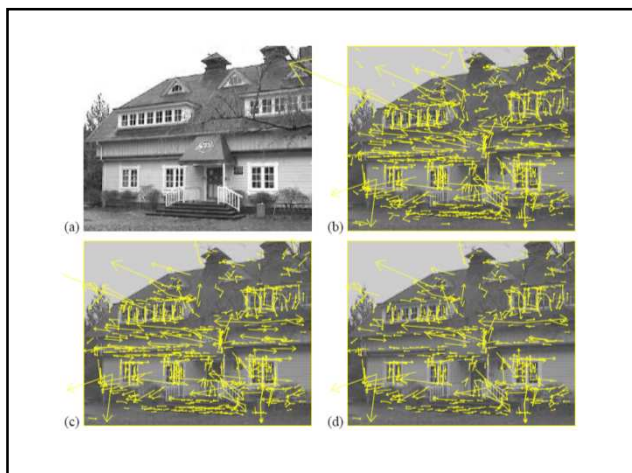
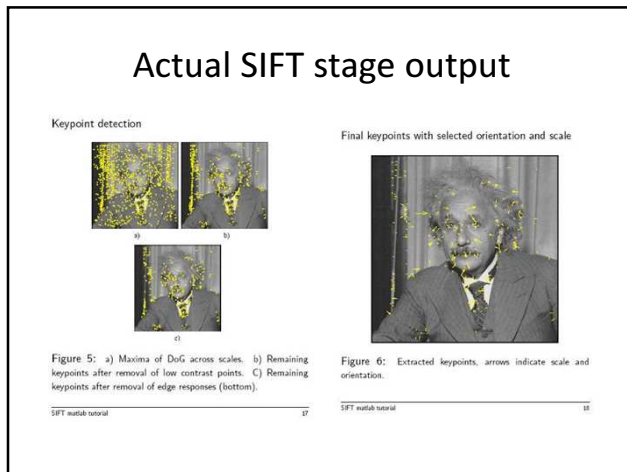
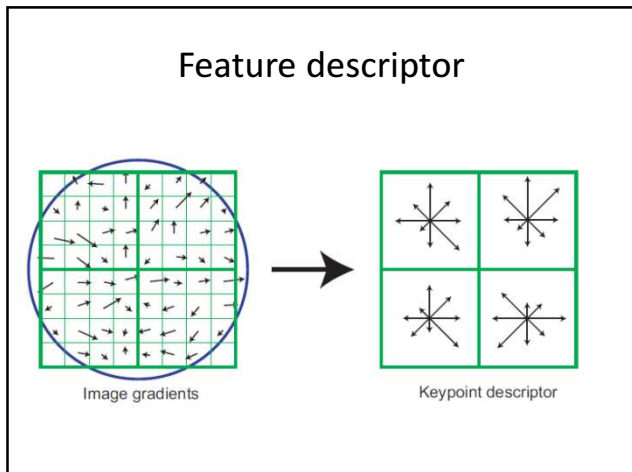
$$= L(x, y, k\sigma) - L(x, y, \sigma).$$



- ### Keypoint localization
- Eliminating extreme points with local contrast
 - Eliminating edge points
 - Similar to Harris corner detector

- ### Eliminating edge points
- Such a point has large principal curvature across the edge but a small one in the perpendicular direction
 - The principal curvatures can be calculated from a Hessian function or covariance matrix of gradient (Harris detector)
- $$H = \begin{bmatrix} D_{xx} & D_{xy} \\ D_{xy} & D_{yy} \end{bmatrix} \quad C = \begin{bmatrix} \sum I_c^2 & \sum I_c I_r \\ \sum I_c I_r & \sum I_r^2 \end{bmatrix}$$
- The eigenvalues of H or C are proportional to the principal curvatures, so two eigenvalues shouldn't diff too much

- ### Finding Keypoints – Orientation
- Create histogram of local gradient directions computed at selected scale
 - Assign canonical orientation at peak of smoothed histogram, achieving invariance to image rotation
 - Each key point specifies stable 2D coordinates (x, y, scale, orientation)
-



- ### How to use these features?
- Distance could be L2 norm on histograms
 - Match by (nearest neighbor distance)/(2nd nearest neighbor distance) ratio

Application: object recognition

- The SIFT features of training images are extracted and stored
- For a query image
 1. Extract SIFT feature
 2. Nearest neighbor matching

Conclusion

- A novel method for detecting interest points. The most successful feature in computer vision
- Histogram of Oriented Gradients are becoming more popular
- SIFT may not be optimal for general object classification