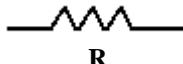
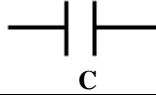



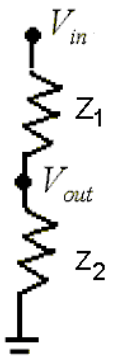
DO NOT WRITE ON THIS SHEET

RETURN SHEET AFTER QUIZ

components	Resistors	Capacitors	Inductors
symbol	 R	 C	 L
general equation	$V_R = I_R R$	$I_C = C \frac{dV_C}{dt}$	$V_L = L \frac{dI_L}{dt}$
combining in series	$R_T = R_1 + R_2 + \dots + R_n$	$\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_n}$	$L_T = L_1 + L_2 + \dots + L_n$
combining in parallel	$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$	$C_T = C_1 + C_2 + \dots + C_n$	$\frac{1}{L_T} = \frac{1}{L_1} + \frac{1}{L_2} + \dots + \frac{1}{L_n}$
impedance	$Z_R = R$	$Z_C = \frac{1}{j\omega C} \sim \frac{1}{f}$	$Z_L = j\omega L \sim f$
frequency $\rightarrow 0$	R	open circuit	short circuit
frequency $\rightarrow \infty$	R	short circuit	open circuit
Stored Energy		$W_C = \frac{1}{2} CV^2$	$W_L = \frac{1}{2} LI^2$

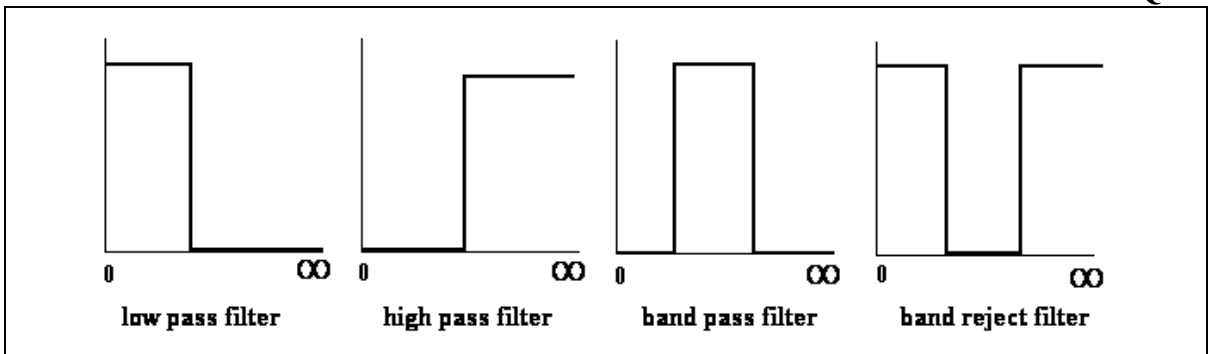
Laws and Rules

Ohm's Law	$V = IR$	
Kirchoff's Voltage Law	Sum of voltages in a loop is zero.	
Kirchoff's Current Law	Sum of currents entering junction equals the sum of currents leaving junction.	
Reading Resistors	XYZ = XY x 10 ^Z ohms	black-brown-R-O-Y-G-B-V-grey-white 0 1 2 3 4 5 6 7 8 9
Reading Capacitors	XYZ = XY x 10 ^Z picofarads = XY x 10 ^(Z-6) microfarads	
suffixes	k (10 ³) M _{eg} (10 ⁶) G(10 ⁹) T(10 ¹²)	m(10 ⁻³) μ(10 ⁻⁶) n(10 ⁻⁹) p(10 ⁻¹²)
	<u>parallel combination shortcut</u> $R_{12} = \frac{R_1 R_2}{R_1 + R_2}$	<u>Power Equation</u> $P = VI = I^2 R = \frac{V^2}{R}$

Voltage Dividers	Sine Waves
 $V_{out} = \left(\frac{Z_2}{Z_1 + Z_2} \right) V_{in}$ $V_1 = \left(\frac{Z_1}{Z_1 + Z_2} \right) V_{in}$ $V_2 = \left(\frac{Z_2}{Z_1 + Z_2} \right) V_{in}$	$v(t) = A \sin(\omega t + \phi) + V_{DC}$ $\omega = 2\pi f \quad f = \frac{1}{T}$ $\phi = -\omega t_0 = -2\pi \frac{t_0}{T}$ $V_{p-p} = 2A \quad V_{rms} = \frac{A}{\sqrt{2}}$

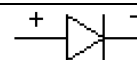
Filters (Characteristic Frequency & Time Constant)

RC Circuit (corner)	RL Circuit (corner)	RLC Circuit (resonant)
$\omega_c = \frac{1}{\tau} = \frac{1}{RC}; f_c = \frac{1}{2\pi RC}$	$\omega_c = \frac{1}{\tau} = \frac{R}{L}; f_c = \frac{R}{2\pi L}$	$\omega_0 = \frac{1}{\sqrt{LC}}; f_c = \frac{1}{2\pi\sqrt{LC}}$

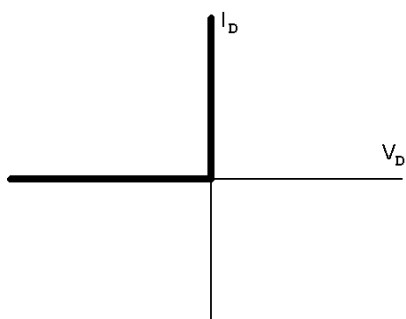


Diodes

1N914 silicon diode: $V_{on} = 0.7$ Volts

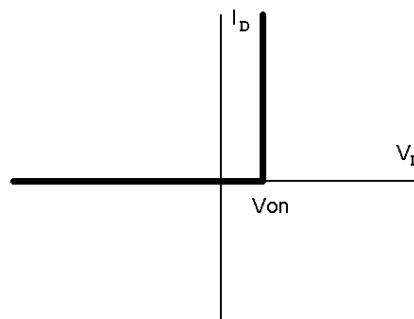


Ideal Diode



$$\begin{cases} On: & V_D = 0 & I_D > 0 \\ Off: & V_D < 0 & I_D = 0 \end{cases}$$

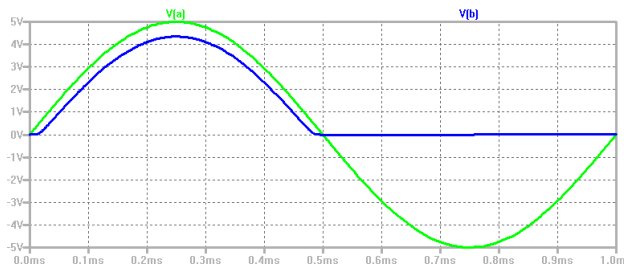
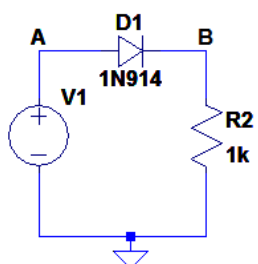
V_{on} Model



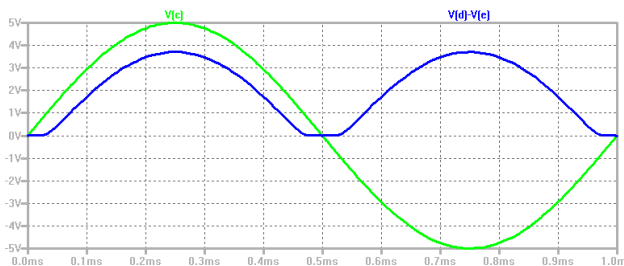
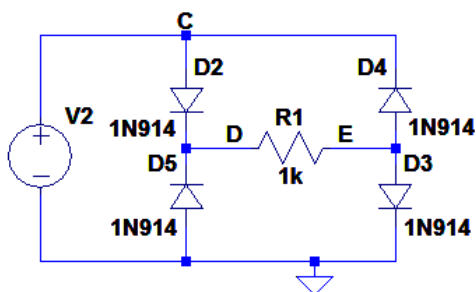
$$\begin{cases} On: & V_D = V_{on} & I_D > 0 \\ Off: & V_D < V_{on} & I_D = 0 \end{cases}$$

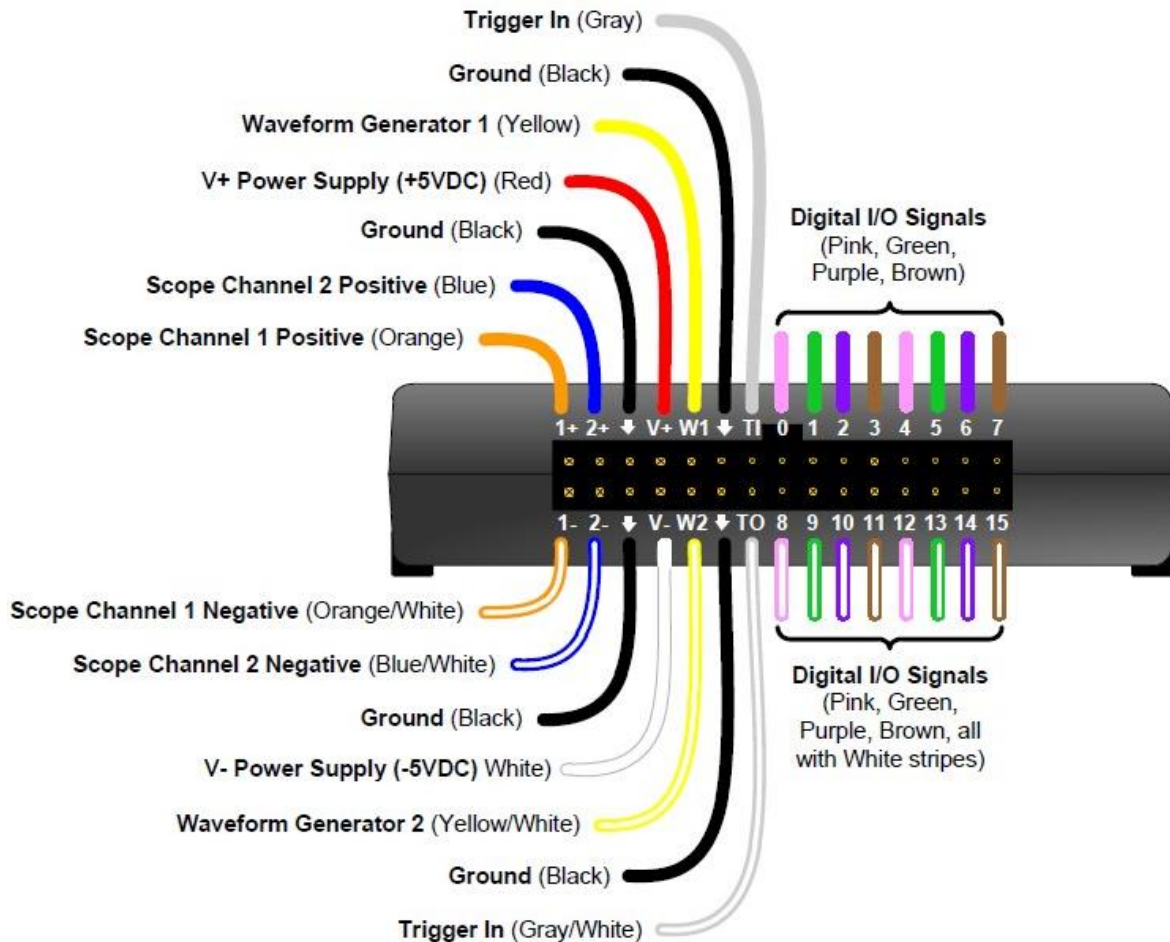
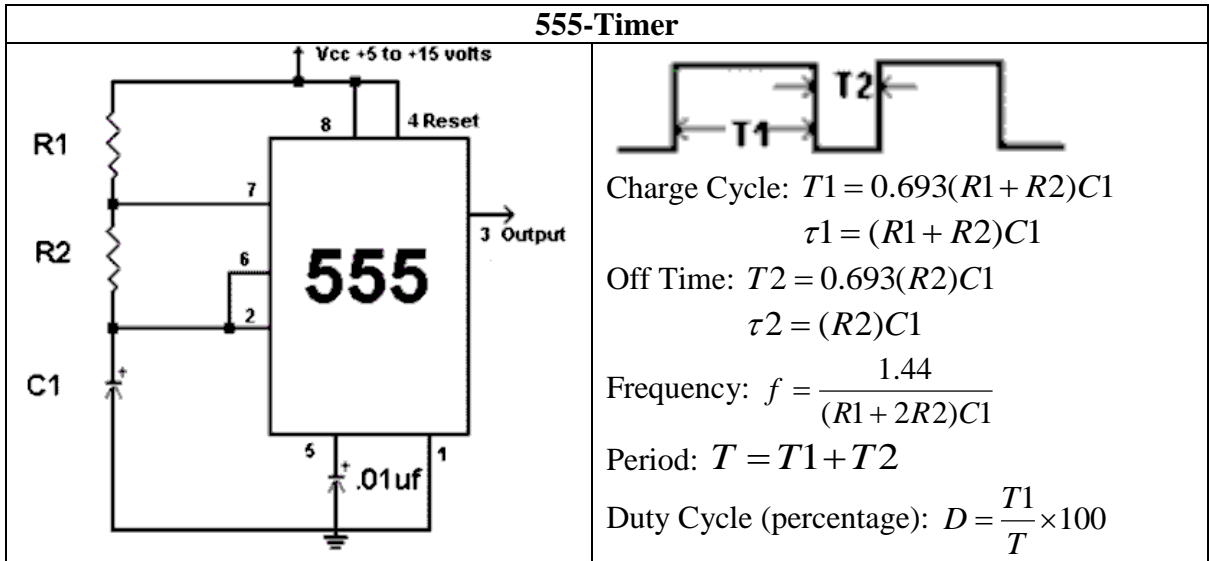
Diode Circuits

Half-Wave Rectifier



Full-Wave Rectifier





Thevenin Voltage Sources		
Find V_{th}	Set load between A and B to open and find $V_A - V_B$	
Find R_{th}	Set voltage sources to shorts and find combined resistance between A and B.	
	$V_L = \frac{R_L}{R_{th} + R_L} V_{th}$	
<p>Experimental Method: Measure output voltage for open circuit (no load) or very large load to obtain V_{th}. Measure output voltage for a series of load resistances. Use the output voltage near $V_{th}/2$ to find R_{th}. Check your answer with another measurement.</p>		

Transistor as a switch		
<p>Transistor circuit</p>	<p>Transistor model</p>	<p>if $(V_i - V_E) < 0.7$</p> <ul style="list-style-type: none"> * transistor is off * switch is open * $I_C = 0 \text{ mA}$ * $V_C = V_{CC}$ <p>if $(V_i - V_E) > 0.7$</p> <ul style="list-style-type: none"> * transistor is on * switch is closed * $I_C \gg I_B$ * $(V_B - V_E) = 0.7$ * $V_{R1} = (V_i - (0.7 + V_E))$ * $V_C = V_E$

Complex Polar Coordinates																	
Complex numbers: $z = x + jy = re^{j\theta}$ ($j = \sqrt{-1}$, $1/j = -j$)	<table border="1"> <thead> <tr> <th colspan="2">phases</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>0</td> </tr> <tr> <td>-A</td> <td>π or $-\pi$</td> </tr> <tr> <td>jA</td> <td>$\pi/2$</td> </tr> <tr> <td>$-jA$</td> <td>$-\pi/2$</td> </tr> <tr> <td>$\tan^{-1}(1)$</td> <td>$\pi/4$ or $-3\pi/4$</td> </tr> <tr> <td>$\tan^{-1}(-1)$</td> <td>$-\pi/4$ or $3\pi/4$</td> </tr> <tr> <td>$x+jy$</td> <td>$\tan^{-1}(y/x)$</td> </tr> </tbody> </table> <p>where A is a constant</p>	phases		A	0	-A	π or $-\pi$	jA	$\pi/2$	$-jA$	$-\pi/2$	$\tan^{-1}(1)$	$\pi/4$ or $-3\pi/4$	$\tan^{-1}(-1)$	$-\pi/4$ or $3\pi/4$	$x+jy$	$\tan^{-1}(y/x)$
phases																	
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$x+jy$	$\tan^{-1}(y/x)$																
Polar to Cartesian transform: $x = r \cos \theta$, $y = r \sin \theta$																	
Cartesian to Polar transform: $r = \sqrt{x^2 + y^2}$ $\theta = \tan^{-1}\left(\frac{y}{x}\right)$																	
$\tilde{V} = \frac{x_1 + jy_1}{x_2 + jy_2} \quad \tilde{V} = \frac{\sqrt{x_1^2 + y_1^2}}{\sqrt{x_2^2 + y_2^2}} \quad \angle \tilde{V} = \tan^{-1}\left(\frac{y_1}{x_1}\right) - \tan^{-1}\left(\frac{y_2}{x_2}\right)$																	
$\tilde{V} = Ae^{j(\omega t + \phi)} = A \cos(\omega t + \phi) + jA \sin(\omega t + \phi)$																	

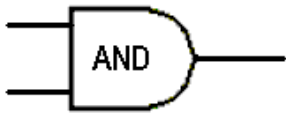
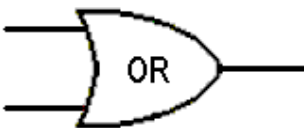
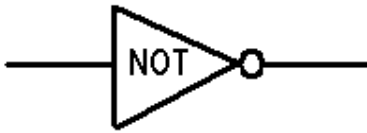

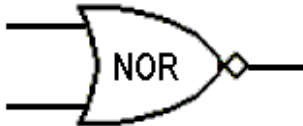

Exponential & Trig Functions		
Euler's Identity $e^{j\theta} = \cos \theta + j \sin \theta$	$V(t) = V_o e^{-t/\tau}$ $\tau = RC$ & $\tau = \frac{L}{R}$	$\frac{d}{dx} e^x = e^x$; $\frac{d}{dx} e^{f(x)} = f'(x)e^{f(x)}$
$e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$	$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} + \dots$	$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} \dots$

Phasor Notation & Analysis	
$V(t) = V_o \cos(\omega t + \varphi) = \text{Re}(V_o e^{j\varphi} e^{j\omega t})$	Phasor: $\tilde{V} = V_o e^{j\varphi}$
$V(t) = V_o e^{-\alpha t} \cos(\omega t + \varphi) = \text{Re}(V_o e^{-\alpha t} e^{j\varphi} e^{j\omega t})$	Phasor: $\tilde{V} = V_o e^{-\alpha t} e^{j\varphi}$

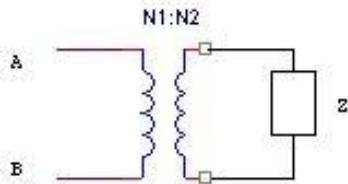
Transfer Functions		
$\tilde{V} = \tilde{I}Z$	$H(j\omega) = \frac{\tilde{V}_{out}}{\tilde{V}_{in}}$	$H(j\omega) = \frac{Z_2}{Z_1 + Z_2}$ series circuit only
Combining Impedances	$Z_{eq} = Z_1 + Z_2 + \dots + Z_N$ series	$\frac{1}{Z_{eq}} = \frac{1}{Z_1} + \frac{1}{Z_2} + \dots + \frac{1}{Z_N}$ parallel
Using Transfer Functions	$A_{out} = H \cdot A_{in}$	$\phi_{out} = \angle H + \phi_{in}$

Decibel Notation	
$dB = 10 \log_{10} \left(\frac{P}{P_o} \right) = 20 \log_{10} \left(\frac{V}{V_o} \right)$	$P = P_o 10^{\frac{dB}{10}}$
$dBm = 10 \log_{10} \left(\frac{P}{1mW} \right)$	$P = (1mW) 10^{\frac{dBm}{10}}$
$dBW = 10 \log_{10} \left(\frac{P}{1W} \right)$	$P = 10^{\frac{dBW}{10}}$

Load Lines	
<p>A load line represents the I-V curve for the combination of the source and resistor. It is used to graphically determine the operating point for devices with nonlinear I-V curves like diodes and transistors.</p>	

Logic Gates														
														
A	B	$Y = A \cdot B$	A	B	$Y = A + B$	<table border="1" style="margin: auto;"> <tr> <td style="text-align: center;">A</td> <td style="text-align: center;">$Y = \bar{A}$</td> </tr> <tr> <td style="text-align: center;">0</td> <td style="text-align: center;">1</td> </tr> <tr> <td style="text-align: center;">1</td> <td style="text-align: center;">0</td> </tr> </table>			A	$Y = \bar{A}$	0	1	1	0
A	$Y = \bar{A}$													
0	1													
1	0													
0	0	0	0	0	0									
0	1	0	0	1	1									
1	0	0	1	0	1									
1	1	1	1	1	1									
														
A	B	$Y = \overline{A \cdot B}$	A	B	$Y = \overline{A + B}$	A	B	$Y = A \oplus B$						
0	0	1	0	0	1	0	0	0						
0	1	1	0	1	0	0	1	1						
1	0	1	1	0	0	1	0	1						
1	1	0	1	1	0	1	1	0						

Boolean Algebra Properties			
$A \cdot 0 = 0$ $A + 0 = A$ $A \cdot 1 = A$ $A + 1 = 1$ $A \cdot A = A$ $A + A = A$ $\overline{\overline{A}} = A$	$A \cdot \bar{A} = 0$ $A + \bar{A} = 1$ $A \oplus B = \bar{A} \cdot B + A \cdot \bar{B}$ $\overline{A \oplus B} = \bar{A} \cdot \bar{B} + A \cdot B$ $A \cdot B = B \cdot A$ $A + B = B + A$	$A + A \cdot B = A$ $A \cdot (A + B) = A$ $A \cdot (\bar{A} + B) = A \cdot B$ $A + \bar{A} \cdot B = A + B$ $\bar{A} + A \cdot B = \bar{A} + B$ $\bar{A} + A \cdot \bar{B} = \bar{A} + \bar{B}$	$A \cdot (B + C) = A \cdot B + A \cdot C$ $A + B \cdot C = (A + B) \cdot (A + C)$ $A \cdot (B \cdot C) = (A \cdot B) \cdot C$ $A + (B + C) = (A + B) + C$ $\overline{A \cdot B} = \bar{A} + \bar{B}$ $\overline{A + B} = \bar{A} \cdot \bar{B}$

Transformers		
	ideal equations	input impedance
	$a = \frac{N_2}{N_1} = \frac{V_2}{V_1} = \frac{I_1}{I_2} = \sqrt{\frac{L_2}{L_1}}$	$Z_{in} = Z_{AB} = \frac{Z}{a^2}$

Op-Amp Circuits

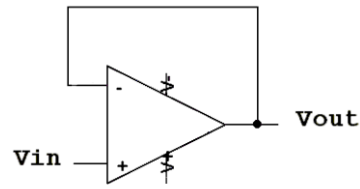
Op Amp Analysis Rules

1. $V_+ = V_-$
2. $I_+ = I_- = 0$

Op-Amp Analysis

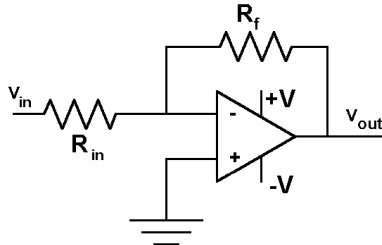
1. Remove Op-Amp
2. Draw a circuit at each input to the op-amp
3. Solve for V_{out} in terms of the input voltage(s).

Voltage Follower



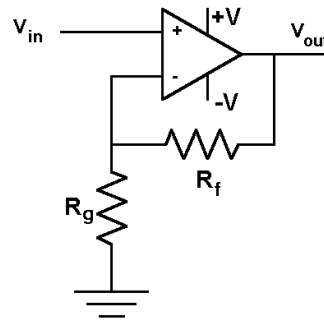
$$A_V = \frac{V_{out}}{V_{in}} = 1$$

Inverting Amplifier



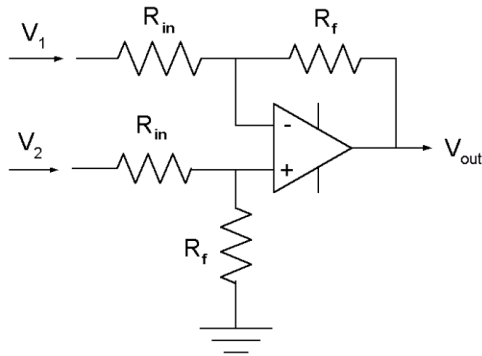
$$A_V = \frac{V_{out}}{V_{in}} = -\frac{R_f}{R_{in}}$$

Non-Inverting Amplifier



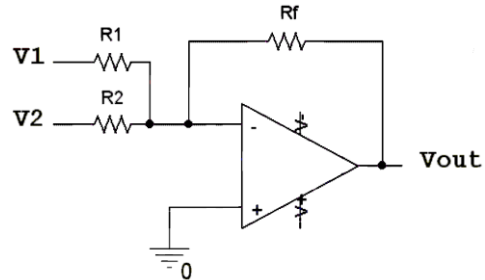
$$A_V = \frac{V_{out}}{V_{in}} = 1 + \frac{R_f}{R_g}$$

Differential Amplifier



$$V_{out} = \frac{R_f}{R_{in}} (V_2 - V_1)$$

Adder



$$V_{out} = -\frac{R_f}{R_1} V_1 - \frac{R_f}{R_2} V_2$$