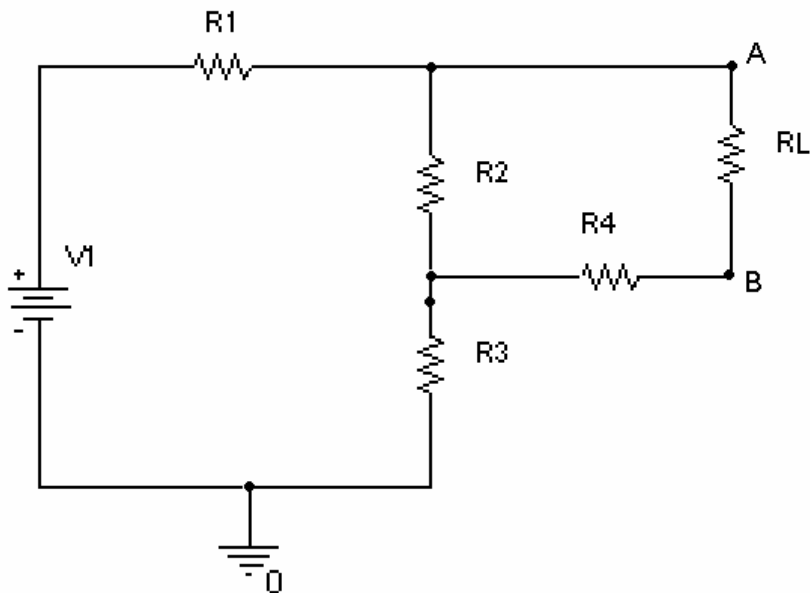


## Questions on Thevenin Equivalent Circuits

*Fall 2004*

### 2. Thevenin Circuits (25 points)



Let  $V_1=12\text{V}$ ,  $R_1=50\text{ ohms}$ ,  $R_2=10\text{K ohms}$ ,  $R_3=2\text{K ohms}$ , and  $R_4=500\text{ ohms}$ .  $R_L$  represents the load placed on the circuit between points A and B.

a) Find the Thevenin voltage between A and B (7 points)

b) Find the Thevenin resistance between A and B (7 points)

c) Draw the Thevenin equivalent to the circuit shown on the previous page. Include the load resistor  $R_L$ . (3 points)

d) What would be the voltage from A to B if  $R_L$  were 2K ohms? (2 points)

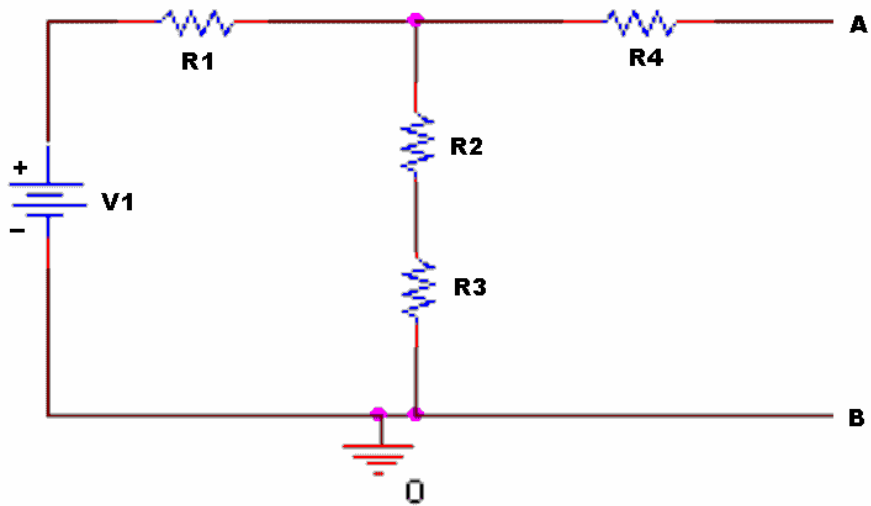
e) What would be the voltage from A to B if  $R_L$  were 10Meg ohms? (2 points)

f) You use the DMM to measure the voltage across the load resistor given in part c (2K ohms) and part d (10Meg ohms). In which circuit would the measured voltage be closer to the voltage you calculated? Why? (4 points)

*Fall 2004 solution  
(none available)*

Spring 2004

2) Thevenin circuits (20 points)



In the circuit above,  $V1=6$  volts.  $R1= 50\Omega$ ,  $R2= 500\Omega$ ,  $R3= 800\Omega$ ,  $R4= 3000\Omega$

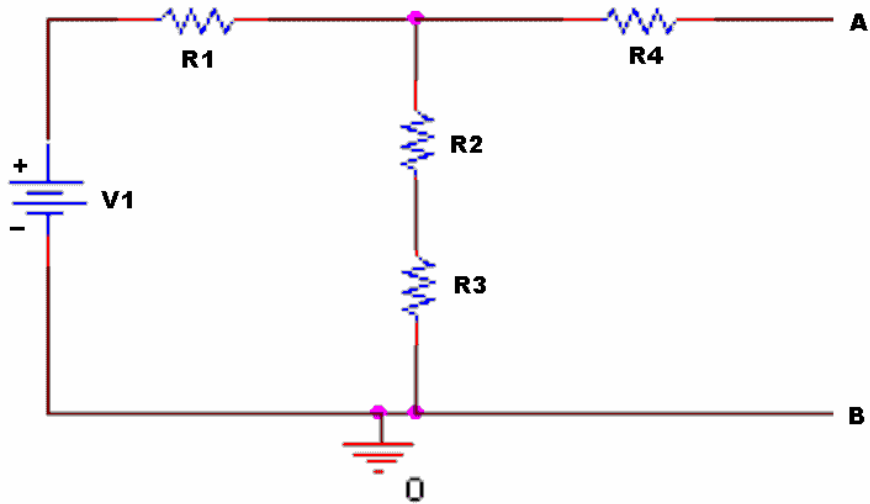
a) Find the Thevenin Voltage ( $V_{oc}$ ) of the Circuit (8 points)

b) Find the Thevenin Resistance (8 points)

c) If you place a load resistor of 2K between A and B, what would be the voltage at point A? (4 points)

Spring 2004 solution

2) Thevenin circuits (20 points)



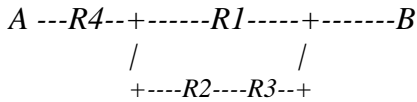
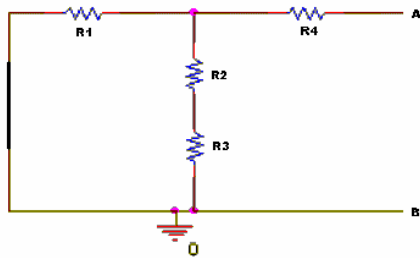
A: In the circuit above,  $V_1=6$  volts.  $R_1= 50\Omega$ ,  $R_2= 500\Omega$ ,  $R_3= 800\Omega$ ,  $R_4= 3000\Omega$

a) Find the Thevenin Voltage ( $V_{oc}$ ) of the Circuit (8 points)

$$V_A = [(R_2+R_3)/(R_1+R_2+R_3)]V_1 = (1300/1350)6 = 5.78 \text{ V} \quad V_B = 0$$

$$V_{th} = V_A - V_B = 5.78 \text{ V}$$

b) Find the Thevenin Resistance (8 points)



$$R_{th} = R_4 + [(R_1 * R_{23}) / (R_1 + R_{23})] \quad R_{23} = 500 + 800 = 1300$$

$$R_{th} = 3000 + [(50 * 1300) / (50 + 1300)] = 3048.15 \text{ ohms} \quad \mathbf{R_{th} = 3048 \text{ ohms}}$$

c) If you place a load resistor of 2K between A and B, what would be the voltage at point A? (4 points)

$$V_A = [R_L / (R_L + R_{th})] V_{th} = [2K / (2K + 3048)] 5.78 = 2.29 \text{ V} \quad \mathbf{V_A = 2.29 \text{ V}}$$

B: In the circuit above,  $V_1=6$  volts.  $R_1= 50\Omega$ ,  $R_2= 1000\Omega$ ,  $R_3= 500\Omega$ ,  $R_4= 2000\Omega$

a) Find the Thevenin Voltage ( $V_{oc}$ ) of the Circuit (8 points)

$$V_A = [(R_2+R_3)/(R_1+R_2+R_3)]V_1 = (1500/1550)6 = 5.806 \text{ V} \quad V_B = 0$$

$$\mathbf{V_{th} = V_A - V_B = 5.806V}$$

b) Find the Thevenin Resistance (8 points) [see pictures for A]

$$R_{th} = R_4 + [(R_1 * R_{23}) / (R_1 + R_{23})] \quad R_{23} = 1000 + 500 = 1500$$

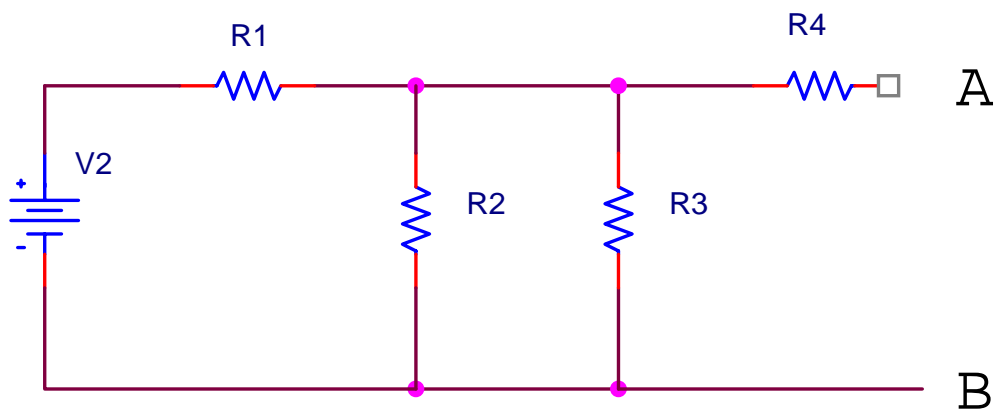
$$R_{th} = 2000 + [(50 * 1500) / (50 + 1500)] = 2048.38 \text{ ohms} \quad \mathbf{R_{th} = 2048 \text{ ohms}}$$

c) If you place a load resistor of 2K between A and B, what would be the voltage at point A? (4 points)

$$V_A = [R_L / (R_L + R_{th})] V_{th} = [3K / (3K + 2048)] 5.81 = 3.45V \quad \mathbf{V_A = 3.45V}$$

Fall 2003

2. Thevenin Circuits (20 points)

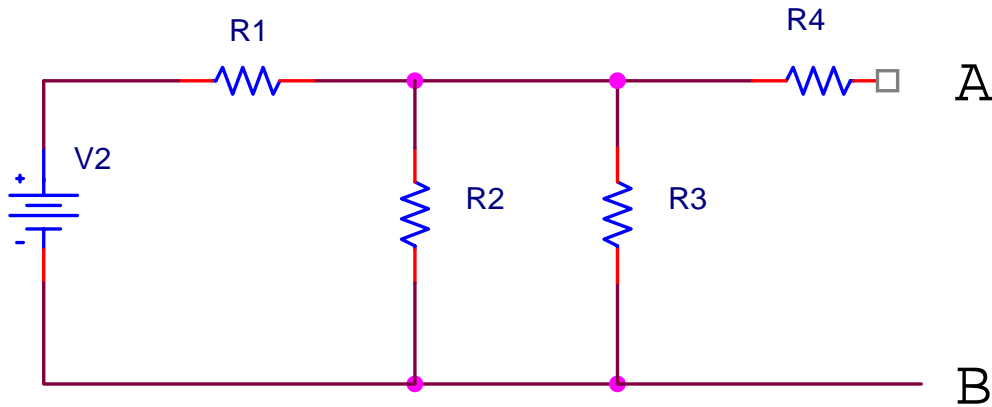


Let  $V_2=12\text{V}$ ,  $R_1=50\text{ ohms}$ ,  $R_2=1\text{K ohms}$ ,  $R_3=2\text{K ohms}$ , and  $R_4=500\text{ ohms}$ .

- c) Find the Thevenin voltage between A and B (8 points)
  
  
  
  
  
  
  
  
  
  
- d) Find the Thevenin resistance (8 points)
  
  
  
  
  
  
  
  
  
  
- e) Draw the Thevenin equivalent circuit with a load of 4K ohms. (4 points)

Fall 2003 solution

2. Thevenin Circuits (20 points)



Let  $V_2=12V$ ,  $R_1=50$  ohms,  $R_2=1K$  ohms,  $R_3=2K$  ohms, and  $R_4=500$  ohms.

f) Find the Thevenin voltage between A and B (8 points)

Test A:  $V_{th} = V_{R_{23}}$   $R_{23} = R_2 // R_3 = 1K * 2K / (1K + 2K) = 0.66667K$

$$V_{AB} = 0.66667K / (0.66667K + 50) (12V) = 11.16V$$

**$V_{AB} = 11.16V$**

Test B:  $V_{th} = V_{R_{23}}$   $R_{23} = R_2 // R_3 = 2K * 0.5K / (2K + 0.5K) = 0.4K$

$$V_{AB} = 0.4K / (0.4K + 50) (12V) = 10.67V$$

**$V_{AB} = 10.67V$**

g) Find the Thevenin resistance (8 points)

Test A:  $R_{th} = R_4 + R_{123}$

$$R_{123} = R_1 // R_2 // R_3 \rightarrow 1/R_{123} = 1/50 + 1/1K + 1/2K \rightarrow R_{123} = 46.5 \text{ ohms}$$

$$R_{th} = 500 + 46.5 = 546.5 \text{ ohms}$$

**$R_{th} = 546.5 \text{ ohms}$**

Test B:  $R_{th} = R_4 + R_{123}$

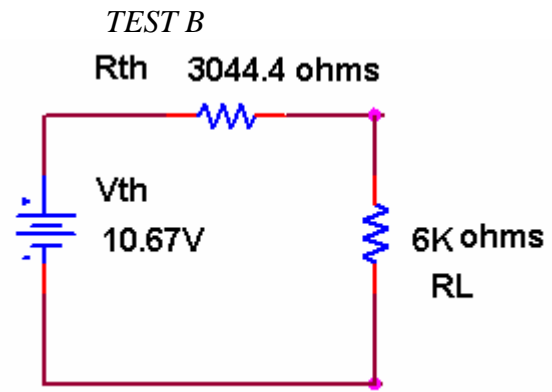
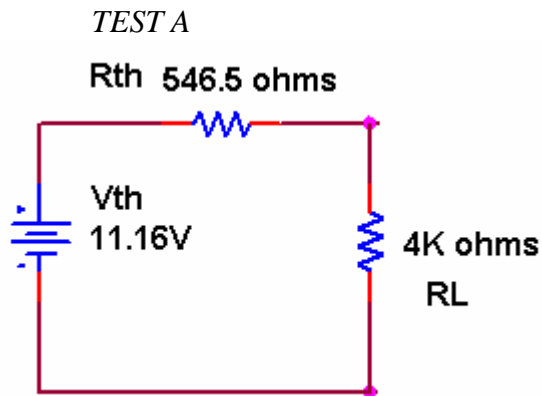
$$R_{123} = R_1 // R_2 // R_3 \rightarrow 1/R_{123} = 1/50 + 1/2K + 1/0.5K \rightarrow R_{123} = 44.4 \text{ ohms}$$

$$R_{th} = 3000 + 44.4 = 3044.4 \text{ ohms}$$

**$R_{th} = 3044.4 \text{ ohms}$**

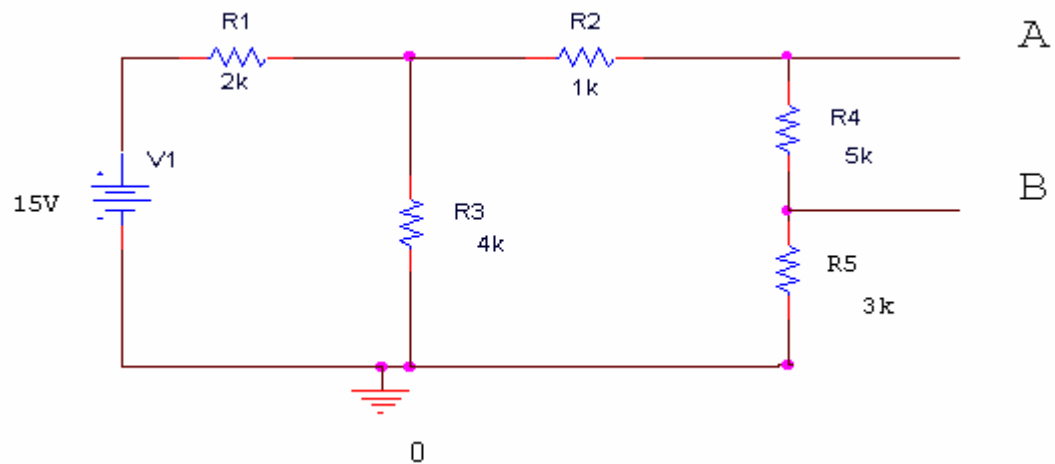


Draw the Thevenin equivalent circuit with a load of 4K ohms. (4 points)



Spring 2003

2. Thevenin circuits (20 points)



a) (6 points) Find the Thevenin voltage ( $V_{oc}$ ) of the circuit assuming the load will be connected between A and B.

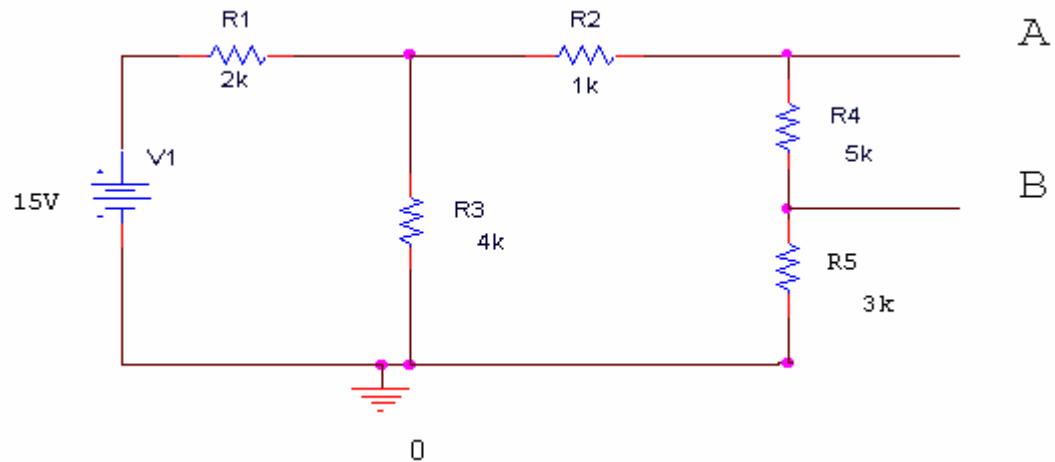
b) (6 points) Find the Thevenin resistance.

c) (4 points) Draw the Thevenin equivalent circuit with a load of 1K ohms.

d) (4 points) Find the voltage between A and B for this circuit with a load of 1K ohms.

Spring 2003 solution

2. Thevenin circuits (20 points)



a) (6 points) Find the Thevenin voltage ( $V_{th}$ ) of the circuit assuming the load will be connected between A and B.

$$R_{245} = R_2 + R_4 + R_5 = 1k + 5k + 3k = 9k$$

$$R_{2345} = R_3 \parallel R_{245} = (9k \times 4k) / (9k + 4k) = 2.77k$$

$$V_{2345} = V_1 (R_{2345}) / (R_1 + R_{2345}) = 15 \times 2.77 / (2 + 2.77) = 8.71 \text{ volts}$$

$$V_4 = V_{2345} \times R_4 / (R_2 + R_4 + R_5) = (8.71 \times 5k) / 9k = 4.84 \text{ volts}$$

$$\underline{\underline{V_{th} = 4.84 \text{ volts}}}$$

b) (6 points) Find the Thevenin resistance.

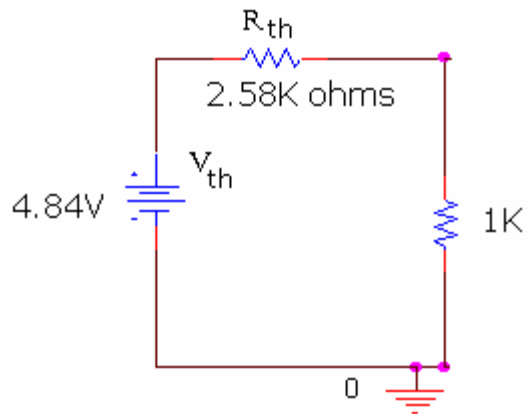
$$R_{13} = R_1 \parallel R_3 = (R_1 \times R_3) / (R_1 + R_3) = (2k \times 4k) / (2k + 4k) = 1.33k$$

$$R_{1235} = R_{13} + R_2 + R_5 = 1.33K + 1K + 3k = 5.33 K$$

$$R_{12345} = R_{1235} \parallel R_4 = (5.33 \times 5) / (5.33 + 5) = 2.58K \text{ ohms}$$

$$\underline{\underline{R_{th} = 2.58 K \text{ ohms}}}$$

c) (4 points) Draw the Thevenin equivalent circuit with a load of 1K ohms.



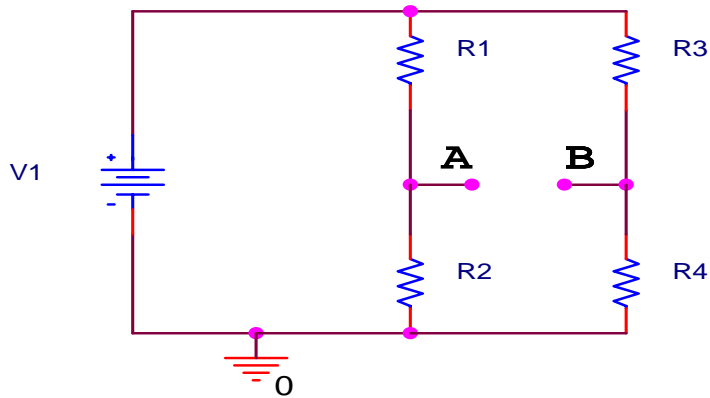
d) (4 points) Find the voltage between A and B for this circuit with a load of 1K ohms.

$$V_{AB} = (V_{th} \times 1K) / (1K + R_{th}) = (4.84 \times 1k) / (1K + 2.58K) = 1.35 \text{ volts}$$

$$\underline{\underline{V_{AB} = 1.35 \text{ volts}}}$$

Fall 2002

2. Thevenin circuits (20 points)



**Given:  $V_1=12\text{ V}$ ;  $R_1=2\text{ k}\Omega$ ;  $R_2=4\text{ k}\Omega$ ;  $R_3= 8\text{ k}\Omega$ ;  $R_4= 4\text{ k}\Omega$**

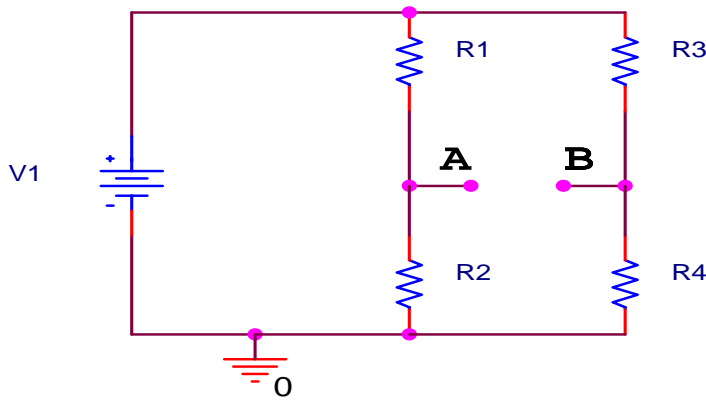
a) Find the Thevenin Voltage ( $V_{oc}$ ) of the circuit assuming the load will be connected between A and B. (6 points)

b) Find the Thevenin Resistance (6 points)

c) Find the current going from A to B if a  $4\text{ k}\Omega$  resistor is connected between A and B. (8 points)

Fall 2002 solution

2. Thevenin circuits (20 points)



Given:  $V1=12\text{ V}$ ;  $R1=2\text{ k}\Omega$ ;  $R2=4\text{ k}\Omega$ ;  $R3= 8\text{ k}\Omega$ ;  $R4= 4\text{ k}\Omega$

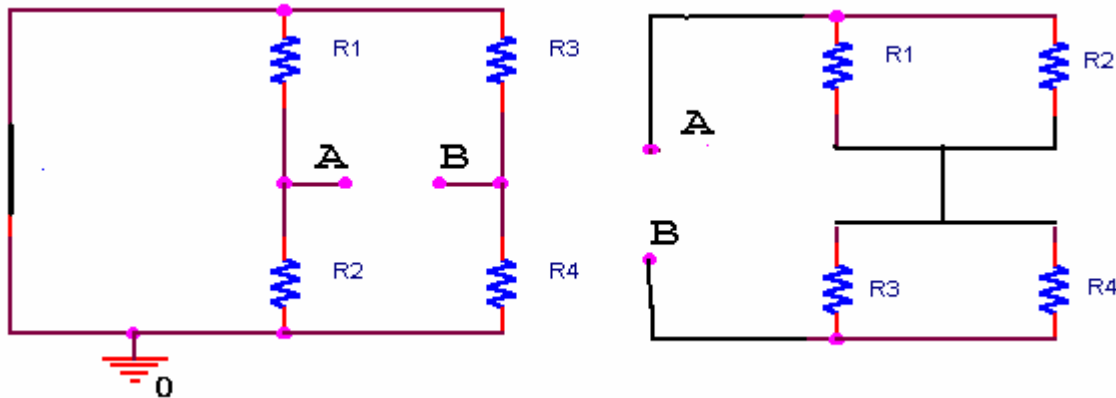
a) Find the Thevenin Voltage ( $V_{oc}$ ) of the circuit assuming the load will be connected between A and B. (6 points)

$$V_{th} = V_A - V_B = V1 \cdot R2 / (R1 + R2) - V1 \cdot R4 / (R3 + R4)$$

$$V_{th} = 12 \cdot 4K / 6K - 12 \cdot 4K / (8K + 4K) = 8 - 4 = 4 \text{ volts}$$

b) Find the Thevenin Resistance (6 points)

Redraw circuit:



$$R_{th} = R1 // R2 + R3 // R4 = R1 \cdot R2 / (R1 + R2) + R3 \cdot R4 / (R3 + R4)$$

$$R_{th} = 2K \cdot 4K / (2K + 4K) + (8K \cdot 4K) / (8K + 4K) = 4/3 + 8/3 = 12/3 = 4 \text{ Kohms}$$

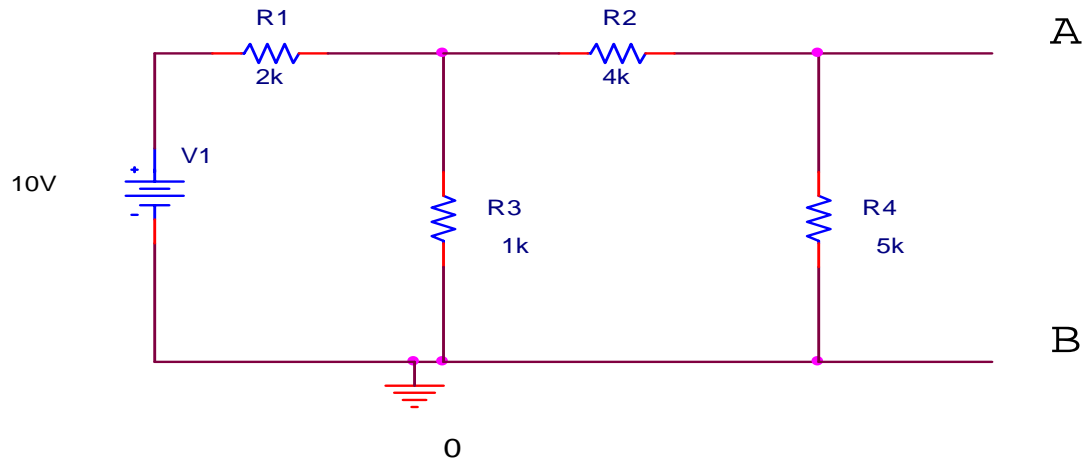
c) Find the current going from A to B if a  $4\text{ k}\Omega$  resistor is connected between A and B. (8 points)

$$V = IR \quad V_{th} = I \cdot (R_{th} + 4K) \quad 4 = I \cdot (4K + 4K)$$

$$I = 0.5 \text{ mamps}$$

Spring 2002

2. Thevenin circuits (20 points)



a) Find the Thevenin Voltage ( $V_{oc}$ ) of the Circuit (8 points)

b) Find the Thevenin Resistance (8 points)

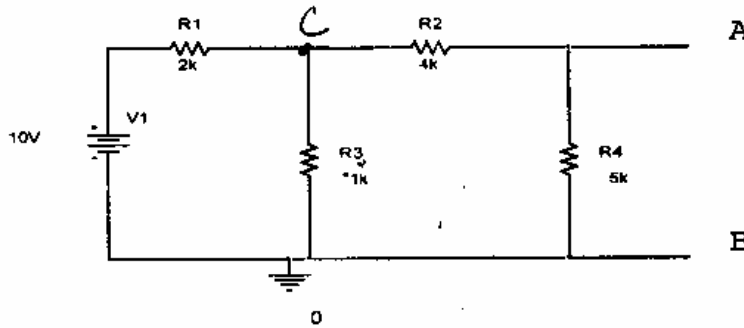
c) Draw the Standard Thevenin Circuit, including a load Resistor (4 points)

Spring 2002 solution

ENGR4300 Test 1A  
Spring 2002

Name \_\_\_\_\_  
Section \_\_\_\_\_

2. Thevenin circuits (20 points)



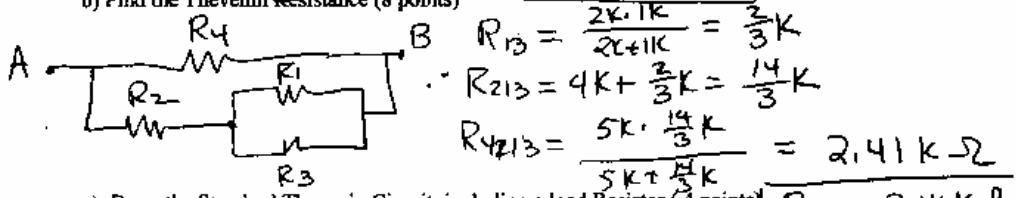
a) Find the Thevenin Voltage ( $V_{oc}$ ) of the Circuit (8 points)

$$R_{24} = 4k + 5k = 9k \quad R_{324} = \frac{9k \cdot 1k}{9k + 1k} = 0.9k$$

$$V_C = 10 \left( \frac{0.9k}{2k + 0.9k} \right) = 3.103V \quad V_A = 3.103 \left( \frac{5k}{4k + 5k} \right) = 1.724V$$

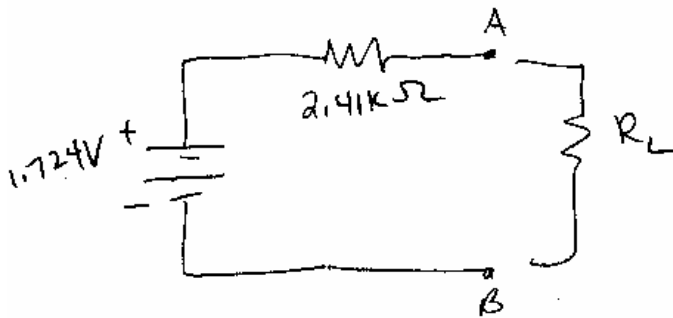
$$V_B = \phi \quad \boxed{V_{AB} = V_{oc} = V_{TH} = 1.724V}$$

b) Find the Thevenin Resistance (8 points)



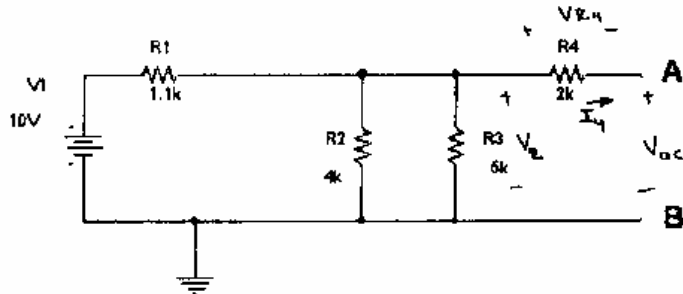
c) Draw the Standard Thevenin Circuit, including a load Resistor (4 points)

$$\boxed{R_{TH} = 2.41k\Omega}$$





2. Thevenin circuits (20 points)



a) Find the Thevenin Voltage ( $V_{oc}$ ) (8 points)

$$V_{oc} = V_2 - V_{R4}, \quad V_{R4} = R_4 I_1 = 0 \Rightarrow V_{oc} = V_2 \quad \left\{ R_{23} = \frac{R_2 R_3}{R_2 + R_3} = 2.22 \text{ k}\Omega \right.$$

$$V_2 = \frac{R_{23}}{R_1 + R_{23}} V_1 = \frac{2.22 \text{ k}\Omega}{1.1 \text{ k}\Omega + 2.22 \text{ k}\Omega} \cdot 10 \text{ V} = 6.69 \text{ V} \Rightarrow \boxed{V_{th} = V_{oc} = 6.69 \text{ V}}$$

b) Find the Thevenin Resistance (8 points)

$$R_{th} = R_4 + (R_1 \parallel R_{23}) = R_4 + \frac{2.22 \text{ k}\Omega \cdot 1.1 \text{ k}\Omega}{2.22 + 1.1 \text{ k}\Omega} = R_4 + 735 \Omega$$

$$= 2 \text{ k}\Omega + 735 \Omega$$

$$\Rightarrow \boxed{R_{th} = 2.735 \text{ k}\Omega}$$

c) Draw the Standard Thevenin Circuit, inserting the values you have found. (4 points)

